Automated detection of filaments in the large-scale structure of the Universe

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ABSTRACT
We present a new method to identify large-scale filaments and apply it to a cosmological simulation. Using positions of haloes above a given mass as node tracers, we look for filaments between them using the positions and masses of all the remaining dark matter (DM) haloes. In order to detect a filament, the first step consists in the construction of a backbone linking two nodes, which is given by a skeleton-like path connecting the highest local DM density traced by non-node haloes. The filament quality is defined by a density and gap parameters characterizing its skeleton, and filament members are selected by their binding energy in the plane perpendicular to the filament. This membership condition is associated to characteristic orbital times; however if one assumes a fixed orbital time-scale for all the filaments, the resulting filament properties show only marginal changes, indicating that the use of dynamical information is not critical for the method. We test the method in the simulation using massive haloes ($M > 10^{14} h^{-1} M_\odot$) as filament nodes. The main properties of the resulting high-quality filaments (which corresponds to $\simeq 33$ per cent of the detected filaments) are (i) their lengths cover a wide range of values of up to $150 h^{-1}$ Mpc, but are mostly concentrated below $50 h^{-1}$ Mpc; (ii) their distribution of thickness peaks at $d = 3.0 h^{-1}$ Mpc and increases slightly with the filament length; (iii) their nodes are connected on average to $1.87 \pm 0.18$ filaments for $\simeq 10^{14.1} M_\odot$ nodes; this number increases with the node mass to $\simeq 2.49 \pm 0.28$ filaments for $\simeq 10^{14.9} M_\odot$ nodes; (iv) on average, the central density along the filaments starts at almost a hundred times the average density in the regions surrounding the nodes and then drops to about a few times the mean density at larger distances, where it remains roughly constant over 20–80 per cent of the filament length (this result may depend on the filament length); (v) there is a strong relation between length, quality and how straight a filament is, where shorter filaments are those characterized by higher qualities and more straight-line-like geometries.

Key words: large-scale structure of Universe.

1 INTRODUCTION
The large-scale distribution of galaxies and dark matter (DM) shows a web-like structure composed by clusters, walls, filaments and void regions, and is usually referred to as the cosmic web. These structures can be easily detected by eye in numerical DM simulations or in the observed distribution of galaxies in large surveys such as the Sloan Digital Sky Survey (SDSS; York et al. 2000).

For clusters and voids, there are several well-established automated identification methods which have been broadly used, such as the friend-of-friends (FOF) algorithm for halo/cluster detection (Davis et al. 1985) and the Padilla, Cecarelli & Lambas (2005) algorithm for reliable detection of voids (see Colberg et al. 2008 for a complete review on different void detection methods). In the case of filaments and walls this task is markedly difficult since, in general, there is still no clear consensus on how to characterize them; filaments and walls show complex 3D shapes.

There are different approaches to the study of filaments. From the theoretical point of view it was found that the gravitational collapse of matter on large scales leads to the formation of sheets and filaments (Zel’dovich 1970). Bond, Kofman & Pogosyan (1996) studied tidal fields in the large-scale structure (LSS) and showed how these produce filamentary structures.

There are several sets of filaments which have been identified and characterized by eye in both simulations and observations. Colberg, Krughoff & Connolly (2005) identified by eye 228 filaments between massive neighbouring haloes in a DM simulation, and described several interesting statistical properties using this sample. In observations, Pimbblet, Drinkwater & Hawkrigg (2004) and Porter et al. (2008) identified filaments in large surveys by eye, and DM filaments were also be detected between clusters of...
galaxies using weak lensing techniques (Mead, King & McCarthy 2010). In X-ray observations, it has also been possible to detect hot gas filaments connecting clusters (Scharf et al. 2000).

The study of statistics and the topology of the galaxy distribution with the aim to search for filaments starts very early, with studies by Zel’dovich, Einasto & Shandarin (1982), Shandarin & Zel’dovich (1983) and Einasto et al. (1984). Options to automate the search of filaments include the use of statistics on the morphology of structures, such as Minkowski functionals, minimal spanning trees (MST), percolation methods and shapefinders (see review by Martínez & Saar 2002). The minimum spanning tree method was introduced in cosmology by Barrow, Sonoda & Bhavsar (1985). This produces a unique graph which connects points of a process without closed loops, but describes mainly the local nearest-neighbour distribution and is unable to provide a full characterization of the LSS. Shapefinders (Sahni, Sathyaprakash & Shandarin 1998) have also been used to identify filaments.

In three dimensions, the morphology of a compact manifold can be characterized by four Minkowski functionals: volume, surface area, integrated mean curvature and integrated Gaussian curvature. It is possible to define a number of quantities related to those functionals; if a set of positions of galaxies or haloes is characterized by particular values of ratios between the Minkowski functionals, it is very likely that it will show a filamentary shape (Bharadwaj et al. 2000), but this does not guarantee a true detection of a filament or that all the selected members actually belong to the filament.

Another algorithm for the detection of filaments was proposed by Pimbblet (2005) based on the assumption that the orientations of constituent galaxies along such filaments are non-isotropic. This method works well on straight filaments with separations smaller than 15 Mpc h$^{-1}$, as has been shown in their application to the Two Degree Field Galaxy Redshift Survey (2dFGRS, Colless et al. 2001).

The Skeleton method (Eriksen et al. 2004; Novikov, Colombi & Doré 2006) has proven useful for the detection of possible filamentary structures in continuous 2D density fields. The skeleton is determined by segments parallel to the gradient of the field connecting saddle points to local maxima. The method involves interpolation and smoothing of the point distribution, introducing the kernel bandwidth as an extra parameter in the procedure of estimating the density field. Extending this work to three dimensions, Soubie et al. (2008) found good agreement between detected skeletons and eye detections in a numerical DM simulation. By using the Hessian matrix eigenvalues they were able to detect filamentary structures (See also Aragón-Calvo et al. 2007a,b). Bond, Strauss & Cen (2009) also use the Hessian matrix of the galaxy density field smoothed on different scales to characterize the morphology of the LSS in mock catalogues and in the SDSS (Stoughton et al. 2002); they use their detected structures to determine the typical scales where filaments, clumps and walls are dominant.

The Candy model used by Stoica et al. (2005) is a 2D marked point process where segments serve as marks. This method has been adapted to three dimensions and also improved to a more general Bisous Model (Stoica, Martinez & Saar 2008), producing detections in very good agreement with the result of eye detection in tracing filamentary structures using only galaxy positions (as in the method we will present). However, the detection and thickness of the resulting filaments is only given by a coverage threshold (per cent of total points, to be included in filaments).

The spin and orientation of haloes in filaments has been studied by Aragón-Calvo et al. (2007b) and Zhang et al. (2009). They use a multiscale morphology filter (MMF) and compute the Hessian matrix eigenvalues in a density field smoothed on different scales, to divide the full volume of their samples into cluster, filament and wall like structures. However, this method, as well as other Hessian matrix based methods, is affected by a lack of an ability to determine the thickness of filaments, and are difficult to apply to observational data, where one needs to define whether a galaxy is a member of a cluster, filament or void.

In this paper, we propose a new automated method to detect filaments which builds upon ideas of several of the methods mentioned previously. A novel feature of the method is that it is designed to search for filaments using nodes (corresponding to haloes or galaxy clusters as in Colberg et al. 2005) selected by applying lower limits on their mass (or proxy for mass). This new method aims to be applicable to discrete halo or galaxy positions even when these are so sparsely distributed that it is not possible to define a smooth density field, or that the Hessian matrix cannot be computed with an adequately high accuracy. This makes it particularly suitable for observational data such as the 2dFGRS or SDSS. In addition, we replace the smoothing scales and filament coverage thresholds by parameters with improved physical meaning. In this new approach a filament quality depends on parameters related to the relative density and gaps of the filament skeleton, and its members are identified as the haloes or galaxies with binding energies with respect to the filament in the plane perpendicular to its skeleton. We will use the numerical simulations to calibrate the binding condition using objects with a collapse time and radius that can be computed even when dynamical information is not available, as is usually the case with observational data. In the latter, measurements or proxies for galaxy masses will still be required in order to define the filament membership condition.

This paper is organized as follows. Section 2 presents the numerical simulation on which we perform our automated search for filaments. The method is presented in Section 3, which also includes details on the measurement of the local density field, and describes the input parameters of the algorithm. Section 4 presents the results and Section 5 concludes this paper with our conclusions.

2 THE NUMERICAL SIMULATION

We use a cosmological DM simulation with parameters corresponding to the concordance lambda cold dark matter ($\Lambda$CDM model, $\Omega_M = 0.045$, $\Omega_{DM} = 0.235$, $\Omega_{DE} = 0.72$, $\Omega_k = 0.72$, $\sigma_8 = 0.847$ and $n = 1$), 500$^3$ particles and a periodic cube side of 250 Mpc h$^{-1}$. At $z = 0$ we find 176 041 haloes and subhaloes in the mass range $1.4 \times 10^{11} < M < 1.5 \times 10^{15} h^{-1} M_{\odot}$, identified using the AHF code (Knollmann & Knebe 2009). For the detection of filaments, we select as nodes a total of 427 haloes with $M > 10^{14} h^{-1} M_{\odot}$. The node pairs that will be the candidates for filament search are constructed using neighbour nodes, which are easily obtained using Voronoi tessellations (VT hereafter, to be explained in more detail in the next section). We obtain a total of 3385 node pairs with separations $<65 h^{-1}$ Mpc, using periodic conditions (310 node pairs straddle the simulation borders); Fig. 1 shows all the node pairs in a slice of the simulation. In the next section we will apply the filament detection method to each of these node pairs.

3 METHOD

Our filament detection method is described in this section. We apply the method to DM halo positions in the simulation as a first step towards the detection of galaxy filaments from observational data.
Automated detection of filaments in the LSS

Figure 1. Density field in the numerical simulation corresponding to a slice 100 $h^{-1}$ Mpc thick. The density is obtained using the halo positions. The red circles enclose the virial radii of the node haloes; white lines connect all the node pairs separated by less than 65 $h^{-1}$ Mpc.

A future extension will also use halo substructure as well as galaxies from a semi-analytic model so as to mimic real galaxies as closely as possible (as galaxies are thought to form in the potential well of DM haloes and subhaloes). When applying our method to semi-analytic galaxies we will be able to detect the effects of using proxies for the host DM halo masses obtained from a galaxy catalogue (e.g. dynamical masses, luminosities in different bands) instead of the measured DM halo masses. Finally, our method can also be extended to use redshift-space information to assess the effect of large-scale bulk motions and the small-scale finger-of-god effect on the resulting filaments.

We will not attempt to find all the filamentary structures in the simulation, only those filament segments generated between haloes above a given mass threshold (node pairs). Therefore, smaller filaments associated to less massive nodes will be missed if they are not in the path (or part) of the selected nodes.

3.1 Density field

In this paper we distinguish between two different definitions of density: (i) the standard DM density traced by the particles in the simulation which we call DM density and (ii) the density given by the halo positions and their virial masses which we call the halo density. It is clear that the halo density contains little information about the mass and structure that lie beyond the virial radii of the haloes, but as we will show it is still an appropriate proxy of the DM density in the simulation. It is clear that halo positions and their masses (or in the observational case, galaxy positions and luminosities) allow a clear by-eye detection of filamentary features at large scales (Colberg et al. 2005).

In general, the density and density gradient field of a distribution of points can be obtained using VT, in a similar approach to that adopted by Aragón-Calvo et al. (2007b) where they compute the density field using Delaunay tessellation field estimator (Shaap & van de Weygaert 2000). In this paper we make use of the neighbour information for all the haloes to trace the halo density field as well as to compute a fast proxy for the halo density gradient vector field. VT also allows us to obtain the immediate neighbours of each halo (or galaxy if applied to observational data). The VT (Voronoi 1908) technique is one of the best adaptive methods to recover a precise density field from a discrete distribution of points, with clear advantage over the method used in smoothed particle hydrodynamics or other interpolation-based techniques (Pelupessy, Schaap & van de Weygaert 2003). We compute the VT for the halo
distribution defining a cellular-like structure, where each halo is associated to a region (or Voronoi cell) in which any point inside this region is nearest to that halo than to any other.

The volume of the Voronoi cell and the enclosed mass define a very precise and adaptive measure of the density. In the case of point masses (such as when using the DM particle distribution), one can measure the exact enclosed mass in each Voronoi cell, and therefore compute a very accurate DM density field. Instead, in this paper we use the halo positions along with their measured virial masses. The VT computation is done in the same way as for particles, but the halo virial mass does not account for all the enclosed mass in the Voronoi cell, it only includes the mass out to the virial radius. For instance, in low-density environments the halo-to-neighbour distance is much larger than the virial radius, and therefore the mass enclosed in the Voronoi cell given by the virial mass of its central halo is underestimated. The opposite occurs in dense environments where the Voronoi cell volume of a halo can be even smaller than their virial sphere due to close neighbours; in this case there is an overestimation of the enclosed mass in the Voronoi cell. As this method does not require absolute density values but only the relative highest density path between nodes (mainly given by the collapsed mass) the use of the halo density would increase the contrast of filaments improving the ability of the method to follow their high relative density path to some degree.

We argue that in the high-density end, the halo density overestimation is not important for our purposes since (i) we will not consider subhaloes or haloes inside the virial radius of nodes (the most massive haloes) and (ii) the inter halo distance becomes comparable to the virial radius at halo densities much greater than the average density along the filaments, and therefore only a few haloes considered in our analysis will suffer this overestimation. As a result, most of the haloes that will present an overestimated density will be nodes, and the remaining affected fraction will be located around nodes and in the central sections of the filaments, where their filament membership will be ensured, independently of the overestimation of their density.

In low-density regions the Voronoi cells of haloes are always much larger than their virial spheres which produces an underestimation of the density; later in this section we will work on diminishing this problem by using an approximation assuming Navarro, Frenk & White (1997, NFW) profiles, to define the characteristic DM density between two haloes.

Before moving on to the calculation of the characteristic density between haloes, we will analyse in more detail the differences between the halo and DM densities. For a smooth density field, such as is the case of fields traced by DM particles, the Hessian matrix can be computed with high accuracy to find the filament components easily. But the process is more complicated in the case of having only the positions of haloes and their virial masses. This is due to the sparse coverage of haloes, their variable masses, and the loss of information regarding the mass located beyond the virial radii of haloes. In order to understand the importance of these issues we will look at the relation between average halo to neighbour separation ($D_{IP}$) and its Voronoi cell volume.

In order to recover the real DM density field as best as possible using only halo positions, one needs to take into account the following.

(i) In high-density environments the Voronoi cell volume is related to the local mean interparticle distance, i.e. the mean neighbour distance $D_{IP}$. The left-hand panel of Fig. 2 shows a very tight relation between these two quantities for the full halo population. In the figure, the dashed line shows the $V \propto D_{IP}^3$ relation, which is very useful for halo detection methods such as FOF (Davis et al. 1985), where the particle separation is used to connect particles above a given density threshold. In the case of having only halo positions, we find that this relation breaks down at lower densities (as can be seen in the left-hand panel of Fig. 2). The origin of this departure from the distance versus volume relation is the complex shapes developed by Voronoi cells at such low densities as result of greater standard deviation in the computation of $D_{IP}$ due to a low neighbour count and interhalo distances falling within a wide range of possible values. Another possibility is that shot noise is affecting

\footnote{We refer as complex cell shapes to non-spherical or non-polyhedric like shapes, produced when having few neighbours at non-uniform distances.}

\begin{figure}
\centering
\includegraphics[width=0.48\textwidth]{left_panel.png}
\includegraphics[width=0.48\textwidth]{right_panel.png}
\caption{Left-hand panel: Voronoi cell volume versus mean neighbour separation, $D_{IP}$, for all the haloes in the simulation. Right-hand panel: Voronoi halo density versus $D_{IP}$ for all the haloes. Dashed lines represent the relation $V = D_{IP}^3$ (left-hand panel); in the right-hand panel it corresponds to $V = \text{median}(M_{\text{VIR}})/\rho$.}
\end{figure}
our estimates, but this should not be the main source in our case since haloes mark the highest peaks in the density field, and we use a relatively large minimum number of particles per halo. This implies that the local clumpiness of a set of haloes in low-density environments is only poorly related to its density; this may pose a challenge to the search for the backbone of filaments. This effect is negligible when obtaining the density field using DM particles since these typically produce a smoother spatial coverage and therefore a much smaller fraction of these will be surrounded by Voronoi cells with complex shapes.

(ii) The spread in the virial masses of the haloes, introduces a scatter in the relation between mean neighbour separation and the halo density (right-hand panel of Fig. 2) with respect to the resulting relation from using only cell volumes. Therefore, the halo density can only be used as a proxy for the matter density, and will serve to choose which halo pair will have the highest local DM density; by choosing the neighbour with the greatest halo density, it will probably be the nearest one and very likely the correct choice. This will sometimes not be true, for example when two or more neighbours have similar halo densities. Consider for example two neighbour cells with almost equal densities, but one having $F$ times more mass and $F$ times more volume than the other ($F > 1$); if we make a simple estimate of the DM density for the region lying between the halo and these two neighbours using NFW profiles for each halo, we will find that the path connecting to the smallest and closest neighbour will have the highest DM density. Later in this section we will apply this correction to our VT density estimates.

We now estimate the local DM density between a halo and its neighbours, which we call the characteristic DM density $\rho^*$. As we have shown, the halo density estimate is relative and it is only used to find the neighbour with the highest local DM density from all the possible halo–neighbour pairs. This density is an approximation that depends on the halo masses and interhalo distances, and therefore it is probably safer not to compare it to the real DM density field given by the DM particles. Due to these considerations, in order to find the path of highest local DM density connecting two nodes, we need to add conditions on when and how to use of the halo density field. To estimate the characteristic DM density $\rho^*$ between the $i$th halo and one of its neighbours, halo $j$, we will have two cases depending on the relation between their separation and their virial radii,

(i) $D_{ij} \leq R_{\text{vir}}(i) + R_{\text{vir}}(j) - \rho^* = k_1 \rho(i)$,

where $D_{ij}$ is the distance between haloes, $\rho$ is the halo density, and $k_1$ is a constant which includes the halo density of halo $i$ common to all its neighbours. The fraction of halo pairs which satisfy this condition is very low and correspond to nodes and their immediate neighbours (haloes which are linked gravitationally); here the halo density is a good proxy for the DM density, and even a possible overestimation of the halo density due to cell volumes smaller than virial spheres is positive for our purpose, since gravitationally linked haloes should have the first priority at the moment of choosing the halo–neighbour path to form the filament skeleton. In this case, the segment connecting haloes $i$ and $j$ will have the maximum characteristic DM density among the other immediate neighbours.

(ii) $D_{ij} > R_{\text{vir}}(i) + R_{\text{vir}}(j) - \rho^* = k_2 \rho(j) \eta^{-1} f(M_i, M_j)$.

Most halo pairs fall in this second case. Here we use NFW profiles to estimate a proxy of the characteristic DM density between two haloes. This proxy consists on the minimum DM density present in the path between two haloes, obtained by extending NFW profiles beyond the halo virial radii (this is a good approximation since the average of the interhalo separation in the filament backbones is $4.80 \pm 0.03$ times the sum of the virial radii of the two neighbour haloes, see Section 4.1). In the equation, $M_i$ and $M_j$ are the halo masses, the $\eta$ factor represents the breakdown of the relation between interhalo distance and Voronoi cell volume,

$$\eta = \frac{D_{\text{vir}}^2}{V_{\text{cell}}}$$

$$f(M_i, M_j) \simeq \left( \frac{M_i}{M_j} \right)^{0.13} \left( \frac{1 + \Omega}{\Omega} \right)^3, \quad \Omega = \left( \frac{M_i}{M_j} \right)^{0.376},$$

and $k_1$ and $k_2$ are constants intended to provide the continuity between both densities at $\eta = 1$, and $\Omega = 1; M^* = 10^{12.5} h^{-1} M_{\odot}$ is the constant in the Bullock et al. (2001) concentration versus mass relation. The $\eta$ parameter appears naturally in this approximation where its value is usually greater than 1; therefore, two haloes with high masses and high Voronoi halo densities will have lower $\rho^*$ if their separation is large, as can be the case in regions with a low number density of discrete points.

The DM density between two haloes will be used as segment weights in the search for the path connecting two nodes, in a similar way to that used in the search for the shortest path in graph theory; therefore, the filament backbone or skeleton is the result of solving for this graph, which has several different approaches in the literature (Biggs, Lloyd & Wilson 1986).

### 3.2 Input parameters

We detect filaments using nodes above a fixed minimum mass. This choice is necessary since the filamentary structure is found at different scales; there are even filaments inside filaments or inside clusters (Bond et al. 1996).

In addition to the minimum node mass, other parameters will be necessary since otherwise it is always possible to find the highest density path connecting any two nodes. However, our aim is to involve only the lowest number of parameters possible, which include the following.

(i) A minimum density threshold for the galaxies or haloes which form the backbone of a filament. This density refers to a minimum characteristic DM density (defined in the previous subsection) along the consecutive halo pairs which form the filament backbone. There is no fixed physically motivated minimum value for this quantity, but we are interested in the filaments which are at least noticeably above the local background density, i.e. filament backbones above a few times the mean density. We will use this minimum density as a quality parameter for the detected filaments, since the higher this density for a filament is, the stronger the density gradients and filament-like potential will be, with more haloes bounded to them.

(ii) A maximum gap threshold for the galaxies or haloes which define the backbone of the filament. A measure of the gaps in a filament is given by max$(D_{\text{SK}}/(D_{\text{vir}}))$, the maximum distance divided by the average distance between all pairs of consecutive skeleton members of an individual filament. Large values for this parameter imply large gaps between two filament sections. Gaps are an important problem, particularly for low-density filaments. Again, this parameter will not define a limit on what is identified as a filament, but will be used as another quality parameter since the smaller this value is, the more continuous and uniform the filament will be, with less noticeable gaps in the backbone.

(iii) After the definition of the backbone or skeleton of the filament has been completed, we select the members of the filament. This is done by analysing which neighbours are gravitationally
linked to the filament and will collapse into the skeleton or remain within the filament for at least a given amount of time. We define a time-scale $t_p$, which is the maximum time allowed for the orbit of a halo in the plane perpendicular to the filament, assuming it is gravitationally bound (in this plane). Since the peculiar velocities of the haloes in the numerical simulation are known, we can calculate which haloes are bound to the filament; we use this information to characterize an average time-scale and the associated radius out to which bound haloes can be found. This will help to implement this filament identification in the case of observational data with no available information on peculiar velocities.

It is complicated to define physically motivated density and gap thresholds for each filament analogous to the virialization density for the spherical collapse model. The reasons behind this are the complicated filament shapes and their continuous feeding of their node haloes or clusters. Therefore, we will use these parameters to assess the quality of a filament; filaments will be better defined if their minimum backbone densities are high and their largest gaps are small.

The reasons behind the choice of these two parameters to define the quality of filaments are the following. A filament is a region in the universe where the gravitational collapse of matter occurs mainly towards a line (continuous but not necessarily straight); therefore, we have a cylindrical-like density profile with its associated cylindrical-like potential. Following this principle, and at the scales we are interested in this paper (filaments between high mass haloes), we will assume a filament is of higher quality than another one if it is more likely to satisfy the previous conditions. A stronger cylindrical-like density profile (indicated by the DM density between consecutive halo pairs in the skeleton) above the background will produce a stronger collapse of matter towards the skeleton, and smaller gaps between filament backbone members will better guarantee the continuity of the filament. The complex geometries and different scales characterizing filaments, along with the facts that there is no known density profile a filament should follow and that they are unstable structures, make it difficult to set the values for these two parameters that will ensure a high-quality sample of filaments. Instead we simply assume that a higher characteristic density and smaller gap parameters imply a higher quality filament.

3.3 Description of the algorithm

Fig. 3 shows a cartoon depiction of some of the steps followed by the algorithm to identify filaments for a particular node pair; in the figure, circles represent halo positions and their virial radii. We identify filaments in the following way.

(i) We select a node tracer pair (indicated by blue circles in the figure).

(ii) We follow the segments of highest local DM density given by the characteristic density $\rho_\star$. This defines the filament backbone or skeleton. For this we define a set of threshold densities $\rho_\star(i)$ with $i = 1, \ldots , N$, in the range set by the minimum and maximum densities in the full density field.

(iii) For each node we generate a list of neighbour haloes just outside the virial radius in the half hemisphere that points to the other node. These neighbours will be labelled as start haloes associated to the node from which we will start the filament search. End haloes will be the neighbours associated with the other node in the node pair in the half hemisphere pointing back to the start node. In panel (a) of Fig. 3, the blue dotted lines indicate the half hemispheres of the nodes that point to the other node; red circles mark the haloes at the start and end nodes.

(iv) The first attempt at identifying a filament is done starting at the highest density threshold $\rho_\star(i = 1)$.

(v) The process is iterative selecting the start halo with the highest local DM density with respect to the start node, characterized by a local density greater than $\rho_\star(i)$. A halo that satisfies this condition becomes part of a possible skeleton, and we search for neighbours of this new skeleton member using the same conditions. If there are no new neighbours satisfying this, we go back to the previous halo from where we will choose a different neighbour to restart the procedure. Panel (b) depicts this step. The colours of the lines (solid and dashed) connecting pairs of haloes correspond to the local characteristic DM density (densities are shown in the colour-scale bar at the bottom of the panels). As can be seen, we start with the maximum characteristic density threshold $\rho_\star(i = 1)$ denoted by a vertical black line in the colour bar. We choose the start halo (the one connecting with the start node located near the bottom of the panel) which has four neighbour candidates (connected by dashed lines to the start halo) for skeleton members, but two neighbours are neglected since they are also start haloes. This leaves two remaining candidates, but none of them are characterized by densities higher than the threshold, and we are not able to find a filament at this density threshold.

(vi) We repeat the last step with a different start halo until any of the end haloes of the other node are reached, or until there are no more haloes satisfying these rules.

(vii) If no connection to the other node is found, we move down to the next lower density threshold step $\rho_\star(i + 1)$, and go back to step versus panel (c) shows the skeleton after lowering several times the density threshold down to the point where the skeleton contains four members (connected by the solid lines). However, the fourth skeleton member has no neighbour candidates (connected by dashed lines to the fourth member) with characteristic DM density greater than the current threshold.

(viii) We will always find a set of connected points (a filament backbone) between two nodes for a sufficiently low value of $\rho_\star$ density. Higher values of this density imply stronger filament contrasts. Panel (d), shows the result when a first skeleton was completed between the two nodes, for a sufficiently low-density threshold.

(ix) We recentre the local centre of mass of the filament skeleton using its immediate Voronoi neighbours.

Having a well-defined backbone, we start adding skeleton neighbours to the filament and computing filament characteristics, in the following way.

(i) For any given halo $k$ we find the nearest skeleton member $j$ (shown in panel e).

(ii) We measure the mass contained in a cylinder around the skeleton at the position of the skeleton halo $j$. The cylinder height is $H = (D_{j+1} + D_{j-1})/2$ and its radius $R = D_{j}$, Using this mass and the difference between the average velocities of the haloes within that cylinder and that of halo $k$, projected in the plane perpendicular to the cylinder, we compute the total halo energy in the plane, $E$. In panel (e) of Fig. 3, the cylinder is depicted by black dashed lines. The cylinder axis (middle black dashed line) is tangent to the filament at halo $j$ as inferred using the two immediate neighbour skeleton members.

(iii) We compute the orbit time $t$ around the cylinder for halo $k$ assuming that the distance $D_{j}$ is the semimajor axis of the orbit. This time-scale only uses information on the potential energy and does not require peculiar velocity data.
Figure 3. Filament detection method steps. Details of each step in text.
(iv) We select all haloes with $E_p < 0$ and calculate their median orbit time $t_1$; we define $r_1$ as the radius containing 80 per cent of these haloes. This sample can only be obtained from haloes with peculiar velocity information.

(v) We select all haloes with $E_p < 0$ and $t \leq t_F$, with $t_F$ a fixed input parameter, and we define $r_0$ as the radius where 80 per cent of these haloes are contained. This defines a sample using $E_p$ measurements and it therefore needs peculiar velocity information to be constructed.

(vi) We select all haloes with $t \leq t_F$, and define $r_2$ as the radius where 80 per cent of these haloes are contained. This selection can be done with position and mass information alone and does not require dynamical information.

(vii) Finally, we also select all haloes with $t \leq t_1$, and we define $r_3$ as the radius containing 80 per cent of these haloes. This selection also requires velocity information and is used to assess the importance of the binding energy condition against that of the orbital time-scales.

All haloes closer to the skeleton than $r_1$ will be selected as filament members in the simulation. Panel (f) of Fig. 3 shows the resulting filament, where blue circles correspond to haloes belonging to the new filament; the remaining nearby haloes are too far away from the filament and do not satisfy the membership conditions.

4 RESULTS

Fig. 4 shows four detected filaments in the simulation, where the halo density projected on to the $xy$ plane is shown in a colour scale, the skeleton is shown as red lines, and the re-centred skeleton as blue dashed lines. The nodes are indicated by circles with radii equal to the halo virial radius. White points denote all haloes lying closer than $r_0$ from the filament skeleton, and blue boxes denote haloes closer than $r_1$. The red triangles are for haloes with $E_p < 0$. All the filaments contain segments with only either a few or no bound haloes, at least according to our definition.

We bear in mind the possibility of undetected bound haloes since in our energy calculation we do not take into account nearby structures other than the filament. In order to produce a more precise energy calculation one would need to use velocities from other sections of the skeleton instead of only from the nearest skeleton section; filaments show a very complex velocity structure where...
nodes sometimes move towards each other (they may merge in the future) or away from each other, making filaments suffer stretching, elongations, torsions and even rotations. However, the incompleteness in the sample of bound haloes should not affect our estimate of the mean effective radius of the filament \( r_1 \), which we use to define filament membership.

In the upper-left and bottom-left panels of Fig. 4 the filaments show excellent density contrasts, but also show a gap (near the top node in the upper-left panel, and near the left node in the bottom-left panel). This shows the importance of adopting a gap parameter that allows the existence of these features in selected filaments to some degree. The filaments in the right-hand panels are of higher quality than those on the left since they do not show important gaps. The section of the filament on the upper-right panel seems not to follow the highest density path due to projection effects (the filament follows a path that enters the page, along the \( z \)-axis).

### 4.1 Filament properties

We apply the method to the numerical simulation described in Section 2, using a minimum skeleton characteristic density \( \rho_{\text{min}} = 3 \rho_{\text{mean}} \) and no gap restriction, limiting the node pairs to relative distances lower than 65 Mpc \( h^{-1} \).

Out of the 3385 node pairs, 1326 are successfully connected via filaments; we will refer to this first identification as the full sample. We select an additional subsample of 467 filaments which satisfy the additional conditions of \( \rho_{\text{min}} \) above the median of the full sample, and \( \max(D_{\text{SK}})/\langle D_{\text{SK}} \rangle \) below the median; this sample is termed the high-quality subsample and contains 33 per cent of the filaments in the full sample. The separation between backbone members in the full and high-quality samples are, on average, \( 4.80 \pm 0.03 \) and \( 4.19 \pm 0.03 \) times the sum of their virial radii, respectively. As was mentioned above, all the detected filaments connect nodes separated by at least the sum of their virial radii. Fig. 5 shows the relation between gap and density parameters for the detected filaments which show clear trends of larger gaps at lower densities.

Fig. 6 shows the dependence of the quality parameters on node separation for the full sample. There are clear correlations, particularly for filaments shorter than 20 Mpc \( h^{-1} \), which suggests that shorter node separations produce higher quality filaments.

When studying the properties of the filaments detected using our automated procedure, it will be useful to compare with a previous detection. In particular, we will use the results from Colberg et al. (2005) who detected 228 filament in a DM simulation by eye using the smoothed DM density distribution. This filament sample cannot be compared directly with our results, since the selection criteria are very different. However, both samples are the result of restricting the search to filaments connecting neighbouring haloes above \( 10^{14} M_\odot \). The main differences between the two samples are as follows: (i) Colberg et al. use the distribution of DM particles whereas we use halo positions; (ii) they look for filaments using the 12 nearest haloes inside cylinders of 7.5 \( h^{-1} \) Mpc of radius aligned along the node-node axis; in our case we look at all possible neighbour node pairs given by the VT with no volume constrain; (iii) Colberg et al. define a true detection based on a visual criterion instead of using quality parameters; (iv) they discard node pair connections when other clusters lie inside the innermost 5 \( h^{-1} \) Mpc.
from the node-node axis, and we discard node pair connections when another cluster is closer than two times its virial radius to the filament skeleton; (v) they divide their sample in straight, off-centre and warped filaments. Therefore, the reader must bear in mind that comparisons between these two samples are not intended to validate any of the two samples, but to find general filament properties which are less sensitive to different selection criteria.

The node pair connections are given by the VT method, which instead of selecting the $n$ nearest neighbours, chooses neighbours such that the line that connects the pair passes only through the Voronoi cell around each node. This ensures that any point along the segment is nearest to one of the two nodes and not to other haloes. The node pair count of the full sample as function of the node separation is shown in Fig. 7 as an orange dashed line (the scale is indicated on the right y-axis). The full sample shows the same fraction for the full sample of quasars, red bars are for the high-quality subsample, and the blue bars are for the Colberg et al. sample detected by eye.

In the case of filaments detected in the 2dFGRS, Pimbblet et al. (2004) find a fractional abundance of filaments similar to our full sample results; however, their selection criteria are also different from the one we have applied to the simulation. In particular, they also identify filaments by eye and use galaxy positions; therefore in order to make an appropriate comparison it would be necessary to apply our method to realistic 2dFGRS mock catalogues, or directly on the 2dFGRS catalogue.

The main properties of the detected filaments are shown in Fig. 8. The top-left panel shows the distributions of $t_f$ (the median orbit time for haloes with $E_p < 0$), where it can be seen that the high-quality filaments are characterized by lower orbit times as expected since these filaments have higher density contrasts and are more concentrated than the full sample. The samples shown in the figure are obtained by setting $t_f = 2t_h$ (vertical red dashed line) which is slightly lower than the median of $t_f$ (indicated by the vertical blue dashed line). This latter value can be used when detecting filaments without dynamical data since the orbit time distributions shown here are relatively narrow (most of the filaments show similar orbital time-scales).

The top-right panel of the figure shows the distributions of the parameters $r_0$ and $r_1$ (line types are indicated in the figure key) described in the previous section. As can be seen, a fixed orbit time produces a narrow distribution of $r_0$ but a wider distribution of $r_1$ which is obtained using $t_f$. However, the peaks of both distributions are located at approximately 1.3 Mpc $h^{-1}$ Mpc. It is also noticeable a very slight shift towards smaller radii for the high-quality subsample in both cases, an effect which is stronger for the $r_1$ parameter, indicating a dependence of the $t_f$ value with the quality of the filaments. Therefore, better quality filaments seem to be more concentrated while preserving similar thicknesses with respect to the filaments in the full sample. In addition, the figure also shows the scale radius $r_c$ computed by Colberg et al. (2005) for their sample of filaments (blue bars). In their notation $r_c$ defines the radius where the density profiles of straight filaments starts to follow a $r^{-2}$ relation. Our definition of $r_1$ indicates a scale radius containing 80 per cent of the bound haloes with orbit times below the median. Even though both definitions are conceptually different, they account for the scale
Automated detection of filaments in the LSS

Figure 8. Distribution functions of properties of the detected filaments. The samples of filaments detected using our automated method are shown in different line types (explained in the key). The statistics from the Colberg et al. (2005) filament sample are shown as barred histograms.

radius where \( \approx 50\text{--}80\text{ per cent of the filament mass is contained. In general, for a given filament, } r_s \text{ is a more precise computation of the edge of the filament, but requires the DM particle distribution to be calculated; } r_1 \text{ is easier to compute since it only requires halo positions; however, it can underestimate the filament edges depending on the density profile and density contrast. Therefore, despite the fact that the comparison is made among two quantities with different definitions, as well as different filament samples, it is interesting to note that the distributions of } r_1 \text{ and } r_s \text{ show similarities; the latter only shows a slight shift towards larger radii. As can be seen, the characteristic radius which defines a filament shows a narrow distribution with preferred values of } 1\text{--}2\, h^{-1}\text{ Mpc, even when using filaments of different quality or using a sample of filaments selected by eye. In all cases, however, the lengths of the filaments are similar and are traced by halo nodes with masses above } 10^{14}\, h^{-1}\, M_\odot.

The bottom-left panel of Fig. 8 shows the distribution of mass for different filament components (line types are show in the figure key); all the distributions are shown for the full sample of filaments.

As can be seen, this tracer node mass selection produces skeletons and filament envelopes less massive than the filament nodes. Both of these two components show similar distributions, with differences only at the low-mass end. Note that when using either } r_0 \text{ or } r_1 \text{ the resulting filament mass is practically the same. This shows that the detection of filaments using a fixed orbit time (when no dynamical information is available) will provide reliable filament mass measurements. In the case of the high-quality filaments, we find that the masses of the skeleton and the surrounding filament shells are lower than for the complete filament sample, since the former are shorter in length (as can be seen in the bottom-right panel of the figure). We find no clear dependence of filament mass on their node masses.

The bottom-right panel of the figure shows the distributions of node pair separation and of filament extension (line types are indicated in the figure). The filament extension is obtained by adding the distances between consecutive filament member positions (i.e. in a discrete number of segments) along the filament. The node
separation is on average smaller than the filament length, which indicates that most filaments are warped.

The distribution of node pair separation peaks at $\approx 32$ Mpc $h^{-1}$ for the full sample, and at $\approx 15$ Mpc $h^{-1}$ for the high-quality subsample. The filament lengths also show a peak at shorter values for the high-quality subsample. When analysing the ratio between these two quantities in both, the full and high-quality samples, it can be seen that regardless of quality, longer filaments are more warped than shorter filaments; i.e. in the full sample, filaments with node separations below $30 h^{-1}$ Mpc are on average 13 per cent larger than their node separation; this value increases to 40 per cent for larger node separations. The filaments studied with Shapefinders in the Las Campanas Redshift Survey (Bharadwaj, Bhavsar & Sheth 2004) are characterized by lengths of 50–80 $h^{-1}$ Mpc. In this paper, we have found shorter high-quality filaments but we have also required node pair separations $< 65 h^{-1}$ Mpc. It should also be borne in mind that in most cases these filaments are only segments of considerably longer structures with more than two nodes (shapefinders are insensitive to the number of nodes in a filament).

Fig. 9 shows the relation between filament thickness ($r_f$) and filament length. The error bars correspond to the standard deviation in the measurement of the median of $r_f$, and are computed using the jackknife method. In the high-quality subsample, we do not include filaments longer than $80 h^{-1}$ Mpc due to low filament counts ($< 10$). As can be seen, there is a trend of thicker filaments for longer filament lengths in both samples (full and high quality). For the high-quality sample, the median value of $r_f$ for filaments with lengths between 0 and 10 $h^{-1}$ Mpc is $1.11 \pm 0.19 h^{-1}$ Mpc, and for lengths between 60 and $70 h^{-1}$ Mpc it is $2.01 \pm 0.29 h^{-1}$ Mpc (a significance of more than $3\sigma$ for a difference between the longest and shortest filament lengths). This dependence can be a consequence of any or several of the following effects: (i) all filaments feed their node haloes and shorter, less massive filaments will exhaust their mass first due to the higher infall velocity and node halo influence over a larger percentage of the filament length (the influence can extend out to several virial radii, Diaferio & Geller 1997), (ii) shorter filaments are straighter than longer ones; therefore, in longer, warped filaments concave zones along the skeleton could attract haloes from larger distances, an effect that would be absent in straight-line filaments. The detailed study of this possibility is beyond the scope of this paper and will be treated in a forthcoming paper on filament shapes and environments and (iii) a higher probability to spuriously assign bound haloes at larger distances from the skeleton for longer filaments, but this is less likely since this effect is also present when using $r_f$ (which does not depend on a computation of energy) as a thickness indicator.

We study the variation of the mass density along the filament skeletons. Fig. 10 shows the average overdensity as a function of the normalized node pair separation. It should be borne in mind that as we use the interpolated Voronoi density obtained from the halo positions and their virial masses, the density only includes a fraction of the total matter (DM particles beyond the virial radii of haloes are not included in this estimate). We exclude filaments with skeletons containing less than six haloes, and the figure only shows half of the filament length since the profiles are symmetrical (on average). The figure shows a similar density profile to those found by Colberg et al. (2005), where the overdensity rises towards node centres, indicating that on average the infall regions of filaments extent up to 20 per cent of the filament length. At larger distances from the nodes, the overdensity remains at nearly constant values of a few times the average density. The high-quality subsample shows a similar profile although with higher density contrasts than the full sample.

We now study the number of filaments connected to individual nodes, and how this depends on the node properties. Fig. 11 shows the fraction of filaments connected to 0, 1, 2, . . . filaments for the full sample (black solid lines), the high-quality subsample (red solid lines) and the Colberg et al. (2005) results (blue bars). The Poisson error amplitudes are shown as dashed lines for the full and high-quality samples. In the full sample, most nodes are connected to 4–6 filaments, indicating that allowing in all the detected filaments without applying any quality constraints does not provide realistic results, bearing in mind the observational (Pimbblet 2005) and numerical simulation (Colberg et al. 2008) results on this statistics. A better agreement with these estimates is obtained when using the
high-quality subsample, in which case most nodes are connected to two filaments (and the distribution is very similar to that from the Colberg et al. 2005 filaments). In general the number of filaments per node is strongly dependent on the quality of the filaments considered; similar quality thresholds are needed in order to make meaningful comparisons. Given that the number density of filaments is three times higher for the full sample than for the high-quality sample (simply due to the total number of objects in each sample) it can be expected that the distribution of filament connections per node will also be a factor of three higher for the full sample, that is ±6 compared to ±2 connections for the full and high-quality samples, respectively (as ±83 per cent of the nodes of the full sample of filaments are connected by high-quality filaments).

Fig. 12 shows the average number of filaments per node as a function of node mass. In all cases this number increases with the node mass. Errors, shown as dashed lines for the full and high-quality samples, are obtained using the jackknife method; errors are not shown for the highest mass bin $M > 10^{15} \text{M}_\odot$ (cyan hatched region) due to the low number of nodes (10) at this end. Nodes in the high-quality subsample are connected to an average of $1.87 \pm 0.18$ filaments for the lowest mass bin, a number that increases to $2.49 \pm 0.28$ for $M \simeq 10^{14.9} \text{M}_\odot$; the significance of this trend is higher than a 3σ level. This behavior was also observed in the 2dFGRS by Pimbblet et al. (2004), and in a numerical simulation (Colberg et al. 2005), clearly indicating that more massive haloes are more likely to have a larger number of connected filaments. This can be associated to the higher amplitude of clustering of more massive haloes characterizing random Gaussian fluctuation fields in a $\Lambda$CDM cosmology (Pimbblet et al. 2004).

There are a number of possible issues which could affect this statistics that need to be borne in mind: (i) we do not use subhaloes, and therefore node pairs closer than the sum of their virial radii could present filaments which we do not detect. Such close pairs will be more abundant for more massive haloes due to their higher local overdensities, therefore these undetected filaments could populate the high mass end of the Fig. 12. (ii) To avoid repeated filament segments, we discard filaments which are closer than $2V_{\text{VR}}$ to a third node, and Colberg et al. (2005) use a fixed value of $5 \text{h}^{-1} \text{Mpc}$ for a similar proximity condition. In both cases we could be missing short filaments in dense environments where nodes are more massive, have larger virial radii and are more strongly clustered; in such places this proximity constraint could be excessive. In order to test this issue, we make a subsample of filaments applying the quality constraints used for the high-quality subsample, but allowing filaments closer to a third node when (i) the node pair separation is less than $10 \text{h}^{-1} \text{Mpc}$, (ii) the minimum density along the filament is greater than 10 times the mean density, (iii) the sum of the virial radii of the nodes is $>2.5 \text{h}^{-1} \text{Mpc}$ and (iv) the filaments are close to straight-line shapes. These modifications, in conjunction with the intrinsic properties of VT for the node pair selection, ensures that it is very unlikely that the short filaments in this new sample are repeated segments of other detected filaments. The reason behind this is that for larger node pair separations, there will be larger distances from a node to node axis to a third node. Otherwise the constraint of a common facet between node pair Voronoi cells would not be fulfilled. This test subsample is shown as green long dashed line in Fig. 12; as can be noticed the relation of filament connections as a function of mass becomes stronger.

### 4.2 Application to observational data

In the case of applying this method to galaxies, we can use luminosities instead of halo masses and detect filaments following the path of highest luminosity density. In this case, as the light of a galaxy is more concentrated than the mass it is safer to assume that the Voronoi density traces that of the luminosity in both, the high and low-density regimes. In this case, the filament quality can be defined using a luminosity density parameter as well as a gap parameter. However, it would become more difficult to measure a filament thickness since in general there would be no information on the mass and, additionally, there seldom is dynamical information to calculate binding energy conditions in galaxy samples.
A possible way to apply this method could use the skeleton brightness and a brightness threshold for filament membership where (i) the distribution of filament thickness and (ii) the relation between filament thickness and length match the results from a DM simulation where the settings on the quality parameters result in similar number densities of filaments. These tests, and an application to observational data from the SDSS are part of a forthcoming paper.

In the case of a sample with estimates of galaxy masses but no dynamical data, such as in nearby galaxies, it would be possible to select filament members assuming that galaxies are bound to the filament, and requiring orbit times lower than \( t_F \). In the simulation, as can be seen in Fig. 8, using a fixed orbit time allows to recover a distribution of \( r_0 \) (see Section 3.3 for the definitions of \( r_0, r_1, r_2 \) and \( r_3 \)) which, although slightly narrower, peaks at the same radius as when using the full energy calculation. Also, the recovery of the filament mass is only mildly affected by the use of \( r_0 \) or \( r_1 \) to select filament members.

Fig. 13 shows the relation between \( r_0 \) and \( r_1 \). As can be seen, there is a linear relation between these quantities for \( r_1 < \text{median}(r_0) \). Filaments in the high-quality subsample show a very similar median \( r_0 \) and a slightly lower median \( r_1 \) than the full sample, an effect that probably arises from the fact that filaments in the high-quality subsample are shorter than in the full sample (see Fig. 8).

In the case of the observational data with masses, but no dynamical information, the method would only provide measurements of \( r_2 \) which, when comparing the vertical long dashed and dotted lines in both panels, can be seen to provide a good approximation to \( r_0 \). As the relation between \( r_2 \) and \( r_1 \) is reliable for thin filaments, \( r_2 < 1.2 \, \text{Mpc} \, h^{-1} \), thick filaments will probably suffer from an underestimation of their real thickness, particularly if their quality is low. Regarding \( r_1 \) (horizontal dotted lines), it can be seen that their median values are very similar to that of \( r_1 \), indicating that if one can estimate the collapse time of bound objects to the filament, the membership obtained using this estimated time will provide a good membership criterion.

**5 CONCLUSIONS**

We presented an automated method to detect filaments in cosmological simulations, using haloes above a fixed mass as tracers of filament nodes. In addition, we proposed possible directions to improve this method to allow its use with observational data. As filaments cannot be treated as virialized structures as in the case of haloes, and as they are characterized by a wide range of lengths, it is a difficult task to identify them automatically. As a result these have been mostly identified by eye. In this paper we detect filaments using an automated algorithm that provides two filament quality parameters: (i) a minimum skeleton characteristic density and (ii) a gap parameter given by the maximum distance between consecutive skeleton neighbours divided by the average consecutive skeleton neighbour distance in individual filaments. A small gap parameter and a high-density parameter ensure the best quality for a filament. The latter condition is equivalent to request a high-density contrast.

In our method we define the width of filaments using the median radius \( (r_1) \) that contains the haloes gravitationally bound to the filament in the plane perpendicular to the filament skeleton, and that are characterized by orbit or collapse times below an upper threshold. An application of the method to data without dynamical information can be done since the radius \( r_1 \) shows a good correlation with \( r_0 \) and \( r_2 \) (\( r_1 \) is obtained assuming that all the galaxies are bound to the filament and computing their orbit times based only on their positions and masses); the members are then selected requiring orbit times below a fixed time \( t_F \). The relation between \( r_1 \) and \( r_2 \) is one to one for thin filaments below \( r_0 \approx 1.2 \, \text{Mpc} \, h^{-1} \); in thicker filaments \( r_2 \) tends to slightly underestimate the actual width of a filament.

We have presented several filament properties which can be studied in observational catalogues such as the SDSS. In particular, a subsample comprising the 33 per cent highest quality filaments in our numerical simulations shows very similar properties to filaments detected by eye in numerical simulations by Colberg et al. (2005).
(i) Filament lengths are mostly concentrated below $50 \, h^{-1} \text{Mpc}$, but can extend to up to $150 \, h^{-1} \text{Mpc}$. (ii) Shorter filaments are characterized by more straight-line geometries than longer filaments. Filaments with node separations below $30 \, h^{-1} \text{Mpc}$ are $13$ per cent longer than the distance between their nodes; this increases to $40$ per cent for larger node separations. (iii) The distribution of filament widths is relatively narrow and shows a clear peak at $d = 3 \, h^{-1} \text{Mpc}$. There are indications of an increase in the filament thickness as the filament length increases. (iv) Nodes are connected on average to two filaments, this number increases slightly with the node mass, reaching $\approx 3$ filaments per node for masses close to $10^{13} \, M_{\odot}$. (v) In the infall region around nodes the average central skeleton density can be as high as a hundred times the mean density; at larger distances the density drops to a few times the mean density, and maintains a roughly constant value along $20$–$80$ per cent of the filament length. (vi) There is a strong relation between length, quality and straightness in the filament shape, where shorter filaments have better quality and are closer to straight-line geometries.

Similarities of the high-quality sample with the Colberg et al. (2005) results seem to indicate that the natural by-eye criteria are strongly related to our quality parameters; a detection by eye selects high-density contrasts and few gaps. We stress the fact that did not intend to match the properties of the Colberg et al. (2005) filaments, instead we simply chose the mean values of minimum density and gap parameters to define our high-quality sample.

The filament properties we have studied in this paper are focused on the general characteristics of filaments. There remain many specific properties of filaments and of their galaxy populations which can be related to several recent results such as (i) the halo clustering dependence on the halo mass and on its formation time (Gao, Springel & White 2005), (ii) the correlations between halo concentration and spin with the local environment (Avila-Reese et al. 2005), (iii) the fact that galaxy spins are strongly aligned along filaments (Pimbblet 2005), (iv) the results using semi-analytic models obtained by González & Padilla (2009) which show several variations of galaxy properties with the local and large-scale environment and (v) other results showing that galaxy formation should be strongly dependent on the large-scale environment starting from their early stages of development, due for example to the delayed reionization of filaments with respect to clusters as shown by hydro-simulations of the intracluster medium (Finlator, Özlü & Davé 2009). A first step will be to compare observational galaxy properties in filaments, in particular their colours, star formation rates and luminosities with results from semi-analytic models, to characterize some of the previously mentioned environment effects.

Several studies of galaxy properties in clusters and voids have opened the possibility to expect important variations in the properties of haloes or galaxies while embedded in filament-like environments, since the populations of galaxies and haloes are very different in voids and clusters. By converging to a standard filament classification and detection method, the study of galaxy properties and halo assembly in filaments can be carried out with great detail to help understand the reasons behind these important population changes.

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