Coherent backscatter and the opposition effect for E-type asteroids

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Abstract. Recently, Harris et al. (Icarus 81, 365–374, 1989) have observed a strong and unusually narrow (HWHM ≈ 0.8° in the yellow) opposition effect for high-albedo asteroids 44 Nysa and 64 Angelina. In this paper, we apply the theory of coherent backscattering of light from discrete random media to interpret this remarkable opposition brightening. It is shown that coherent backscattering of sunlight from a regolithic layer composed of submicrometer-sized grains with an index of refraction close to that of the mineral enstatite can be a reasonable explanation of the observed opposition effect.

1. Introduction

The shadowing models by Hapke (1986) and Lumme and Bowell (1981) have been widely used to interpret the opposition brightening exhibited by many atmosphereless solar system bodies. Nevertheless, as was noted by Buratti (1991), more extensive laboratory measurements of the bidirectional reflectance properties of various materials are necessary to understand how physically realistic it is to compare astronomical and spacecraft observations with these models. Moreover, there are situations in which the formal fit of theoretical curves to observational data becomes impossible or physically meaningless. Indeed, the opposition effect observed for Saturn’s A- and B-rings (Franklin and Cook, 1965) and icy outer planet satellites (Brown and Cruikshank, 1983; Goguen et al., 1989; Domingue et al., 1991; Thompson and Lockwood, 1992) at visible and near-infrared wavelengths has the angular semi-width of only a few tenths of degree. Such a narrowness of the opposition effect, if explained on the basis of the shadowing models, implies an unrealistically low volume density of the upper, optically active regolithic layer. Recently, Harris et al. (1989) (see also Lagerkvist et al., 1992) have measured a similar opposition effect for high-albedo asteroids 44 Nysa and 64 Angelina (Fig. 1) and concluded that, apparently, the well-known shadowing mechanism cannot reproduce satisfactorily this unusual opposition brightening.

Kuga and Ishimaru (1984) and O’Donnell and Mendez (1987) were the first to mention the opposition effect of the lunar surface near full moon in the context of the so-called coherent backscattering mechanism. Later, in an astronomical publication, Shkuratov (1988) suggested that coherent backscattering may play a role in producing the opposition brightening exhibited by a wide class of atmosphereless solar system bodies. Recently, Muinonen (1989, 1990) mentioned the opposition effect observed for Saturn’s rings and the asteroid 44 Nysa as especially unusual and, probably, produced by the coherent backscattering mechanism, while Hapke (1990), Hapke and Blewett (1991) and Domingue et al. (1991) pointed out the coherent backscattering mechanism as possibly relevant to the strong and narrow opposition effect observed for icy outer planet satellites. Finally, Hapke et al. (1992) have found experimental evidence that coherent backscattering can contribute to the opposition effect of even such a low-albedo object as the Moon. However, no attempt has been made by these authors to apply relevant physical theories to quantitatively analyze the observed opposition phenomenon.

Coherent backscattering has been observed in laboratories for two kinds of scattering media, specifically for rough surfaces (e.g. McGurn, 1990; Maradudin et al., 1992) and media composed of randomly positioned discrete scattering particles, e.g. powder-like layers or suspensions of latex particles in water (Kuga and Ishimaru, 1984; van Albada and Lagendijk, 1985; Wolf and Maret, 1985; Ettema et al., 1986; Kaveh et al., 1986). Unfortunately, theoretical and experimental results relevant to enhanced backscattering from random dielectric surfaces are extremely scarce. [Note that a freshly smoked magnesium oxide (MgO) sample studied by Kim et al., 1990, was in fact a powder-like, three-dimensional discrete random medium rather than a real rough surface. Correspondingly, the measurements for this sample differ dramatically from the measurements by Sant et al., 1989,
The theory of coherent backscatter from discrete random media contains only reproducible parameters, has a rigorous theoretical background, and is in good quantitative agreement with the results of controlled laboratory experiments (see, e.g., Akkermans et al., 1988; Wolf et al., 1988; van der Mark et al., 1988; Mishchenko, 1991c). In recent papers (Mishchenko and Dlugach, 1992b; Mishchenko, 1992b), we have shown that coherent backscatter from sunlight from a regolithic layer composed of submicrometer-sized ice grains is a likely explanation of the opposition effect exhibited by Saturn's A- and B-rings and icy outer planet satellites. It is the aim of the present paper to demonstrate that coherent backscatter can also explain the unusually narrow opposition effect observed for the asteroids 44 Nysa and 64 Angelina. For the reader's convenience, Section 2 will provide a brief introduction to the theory of coherent backscatter of light from discrete random media. For a much more thorough review of the subject, we refer the reader to Barabanenkov et al. (1991). Model calculations will be reported in Section 3. Finally, in Section 4 the principal results of the paper will be summarized and discussed.

2. Theory

To demonstrate the interference nature of coherent backscatter, let us first consider a half-space of randomly positioned scattering particles illuminated by a scalar plane wave incident in the direction given by the unit vector \(\hat{n}\) (Fig. 2). Let the direction of the reflected wave be given by the unit vector \(\hat{n}'\). Consider two light-scattering paths shown in Fig. 2 by solid and dashed lines. These paths involve the same group of \(N\) scatterers, denoted by their positions \(x_1, \ldots, x_N\), but the order of the scatterers is reversed. The waves scattered through the two paths will interfere, the interference being constructive or destructive depending on the phase difference between the paths \(k(\hat{n} + \hat{n}') (x_N - x_i)\), where \(k = 2\pi / \lambda\) is the wavenumber, and \(\lambda\) is the wavelength. Relatively far from the retro-reflection direction, the waves scattered by different groups of particles through the conjugate couples of light paths will interfere in different ways, and, due to the randomness of the medium, the average effect of interference

![Fig. 2. Schematic explanation of coherent backscattering](image)
will be zero. Nevertheless, at exactly the backscattering direction \((\mathbf{n} = -\mathbf{a})\), the phase difference between the conjugate light paths is identically equal to zero for any group of particles, and coherence is completely preserved. Owing to reciprocity, at exactly the backscattering direction, the amplitudes of the two light paths shown in Fig. 2 are equal \((A_1 = A_2)\), and the reflected intensity is \(|A_1 + A_2|^2 = 4|A_1|^2\). In the absence of phase coherence, we would have for the backscattered intensity \(|A_1|^2 + |A_2|^2 = 2|A_1|^2\). Since the scattering paths that involve only one particle do not contribute to the coherent return (there is no reversed path), we conclude that, in the scalar approximation, coherence results in a backscattering peak of amplitude somewhat less than twice the incoherent intensity. More specifically, the backscattering enhancement factor \(\zeta\) defined as the ratio of the total backscattered intensity to the incoherent (diffuse) intensity is given for exactly the backscattering direction by:

\[
\zeta = \frac{I^D + I^C}{I^D} = 2 - \frac{I^D}{I^C},
\]

where \(I^D\) is the diffuse intensity, \(I^C\) is the coherent contribution, and \(I^C\) is the contribution of the single-scattering paths.

Each of the two light scattering paths shown in Fig. 2 goes through each of the particles \(x_1, \ldots, x_8\) only once. In the theory of multiple scattering of waves in discrete random media, such self-avoiding paths give rise to the so-called ladder and cyclical diagrams (see, e.g., Tsang et al., 1985). The sum of the ladder diagrams describes the diffuse intensity \(I^D\), while the sum of the cyclical diagrams describes the coherent contribution \(I^C\). Unlike the diffuse intensity which is a slowly varying function of the phase angle \(\alpha\) (the angle between the vectors \(\mathbf{n}\) and \(-\mathbf{a}\)), the coherent contribution is nonzero only in the nearest vicinity of the pure backscattering direction. The contribution of all the other scattering paths, which go through the same scatterers more than once, is very small as compared with the contribution of the self-avoiding paths like those shown in Fig. 2 and may be neglected (e.g. Ishimaru, 1978). Furthermore, under particular conditions which will be discussed later, the incoherent intensity can be found by solving the common radiative transfer equation (Chandrasekhar, 1960; Ishimaru and Tsang, 1988). Calculation of the coherent contribution is a more difficult problem studied, e.g. by van der Mark et al. (1983), Gorodnichev et al. (1989, 1990), and Ozrin (1992a). However, as discussed above, at exactly the backscattering direction the coherent contribution is simply equal to the incoherent intensity minus the singly scattered intensity.

Although the scalar approximation gives reasonably good results in calculating the copolarized reflected intensity for linearly polarized incident light and in calculating the reflected intensity in the helicity-preserving channel for circularly polarized incident light (e.g. Etemad et al., 1987; Wolf et al., 1988), it does not take into account the vector character of light and, thus, provides only a simplified understanding of coherent backscattering. In particular, the scalar approximation completely fails in calculating the reflected intensity in the practically important case of unpolarized incident light (Mishchenko and Dlugach, 1992a).

In accordance with the vector nature of light, the scalar intensity must be replaced by the four-component Stokes vector \([\mathbf{I}]\) having the Stokes parameters as its components, as follows:

\[
[I] = \begin{bmatrix}
I \\
Q \\
U \\
V
\end{bmatrix}.
\]

(2)

The Stokes vector of the reflected light \([\mathbf{I}']\) is given by:

\[
[I'] = [R][I],
\]

(3)

where \([R]\) is the \((4 \times 4)\) reflection matrix, and \([I]\) is the Stokes vector of the incident light. As in the scalar case, the diffuse component of the reflection matrix \([R^D]\) can be calculated by using the vector radiative transfer theory (e.g. Hansen and Travis, 1974; Hovenier and van der Mee, 1983; Tsang et al., 1985). On the other hand, calculation of the coherent component \([R^C]\) is a more difficult problem which is rigorously solved only for particles much smaller than the wavelength, i.e. Rayleigh scatterers (Ozrin, 1992b). However, as was shown by Mishchenko (1992a), at exactly the backscattering direction the coherent component \([R^C]\) can be rigorously expressed in terms of the matrix \([R^C] = [R^D] - [R^C]\), where, as earlier, \([R^C]\) is the contribution of the singly scattered light. The matrix \([R^C]\) describes the diffuse contribution of all the self-avoiding paths that include more than one scatterer, i.e. the contribution of all the ladder diagrams of orders \(N \geq 2\). For macroscopically isotropic scattering media, this expression has the form:

\[
[R^C] = \begin{bmatrix}
R_{11} & R_{12} & 0 & 0 \\
R_{12} & R_{22} & 0 & 0 \\
0 & 0 & R_{33} & R_{34} \\
0 & 0 & -R_{34} & R_{44}
\end{bmatrix},
\]

(4)

with:

\[
R_{11} = \frac{1}{4}[R_{11}^L + R_{22}^L + R_{33}^L + R_{44}^L],
\]

(5)

\[
R_{12} = \frac{1}{4}[R_{11}^L + R_{22}^L + R_{33}^L - R_{44}^L],
\]

(6)

\[
R_{33} = \frac{1}{4}[-R_{11}^L + R_{33}^L + R_{33}^L + R_{44}^L],
\]

(7)

\[
R_{34} = \frac{1}{4}[R_{11}^L - R_{22}^L + R_{33}^L + R_{44}^L].
\]

(8)

Thus, for the case of unpolarized incident light, the scalar formula (1) for the backscattering enhancement factor \(\zeta\) at exactly the backscattering direction is replaced by the vector formula:

\[
\zeta = \frac{[R_{11}^L + R_{11}^L + R_{11}^C]}{[R_{11}^L + R_{11}^L]} = \frac{[R_{11}^L + R_{11}^L + \frac{1}{4}(R_{11}^L + R_{22}^L - R_{33}^L + R_{44}^L)]}{[R_{11}^L + R_{11}^L]}.
\]

(9)

The expression (4) is a direct consequence of the vector theory of multiple wave scattering in discrete random media and is based on Saxon’s (1955) reciprocity relation for the single-scattering amplitude matrix. As was demonstrated by Mishchenko (1991c), this theory is in good quantitative agreement with the controlled laboratory
measurements made by Wolf et al. (1988) and van Albada et al. (1988) for densely packed latex particles in water illuminated by linearly polarized incident light. Also, for the case of circularly polarized incident light and the helicity-preserving channel, this theory predicts the enhancement factor of exactly two regardless of the effects of finite geometry and absorption, which is in full agreement with measurements of Etemad et al. (1987). Finally, calculations by Mishchenko (1991c, 1992a) for point-like particles show complete agreement with the numbers given by Ozrin (1992b) on the basis of his rigorous vector theory of coherent backscattering by Rayleigh scatterers.

Thus, the calculation of the amplitude of the coherent opposition effect consists of two steps. First, the diffuse reflection matrix [R] and the single-scattering contribution [R'] are calculated by using the well-known numerical methods of the radiative transfer theory. At present, numerical calculations are possible for spherical (Hansen, 1971; Hansen and Travis, 1974; de Haan et al., 1987) as well as for randomly oriented nonspherical (Mishchenko, 1991a,b; Wauben and Hovenier, 1992) particles. Subsequently, equation (9) is used.

It must be noted that the use of the radiative transfer theory to calculate the diffuse component of the reflection matrix and the use of equation (9) to calculate the backscattering enhancement factor imply that the scattering medium consists of uncorrelated, independently scattering particles. In this case, the longitudinal component of the electric field becomes negligibly small. However, as was demonstrated by Mishchenko (1991c) by comparing theoretical calculations with results of controlled laboratory experiments, the approximation of independent scattering gives good quantitative results even for rather densely packed media. Furthermore, as was shown by Tsang et al. (1990), for densely packed media the incoherent component of the Stokes vector of multiply scattered light is a solution of an equation which has the same form as the classical radiative transfer equation and contains the same phase matrix, but the extinction coefficient and single-scattering albedo are modified. However, for the diffuse reflection matrix of a semi-infinite nonabsorbing medium, this modified radiative transfer equation gives exactly the same results as the classical radiative transfer equation. Since calculations reported in the next section are made for optically thick (semi-infinite) media composed of nonabsorbing particles, we expect that the accuracy of our computations is good enough for the purposes of interpretation.

We stress here that the theory developed by Mishchenko (1992a) is based, in the last analysis, on Maxwell’s equations. Although it includes a simplifying assumption of independent scattering, this assumption is explicit and is not accompanied by the introduction of adjustable model parameters without definite physical meaning. The same is true for the radiative transfer theory, which is a direct consequence of the Bethe-Salpeter equation under the ladder approximation for independent scatterers (Barabanenkov, 1975; Prishivalko et al., 1984; Tsang et al., 1985).

Thus, the radiative transfer theory and equation (9) enable us to rather accurately calculate the intensity of the reflected light both in the centre of the coherent opposition peak and outside the peak. To have more complete specification of the peak, we must also calculate its half-width at half-maximum (HWHM). As was rigorously shown by Ozrin (1992b) for the case of a semi-infinite medium composed of nonabsorbing Rayleigh (point-like) scatterers and illuminated by a parallel beam of light incident perpendicularly to the boundary of the medium, the coherent component of the reflected light in the vicinity of exactly the backscattering direction depends on the phase angle θ only through the angular parameter q = klz, where l is the scattering mean free path of photons in the medium. Figure 3 shows the angular profile of the backscattering enhancement factor ζr calculated on the basis of the Ozrin theory for the case of unpolarized incident light (Mishchenko, 1993). Note that ζr(0) ≈ 1.54 (cf. Mishchenko, 1992a). It is seen from this figure that the HWHM of the coherent opposition peak is given by:

\[ \text{HWHM} \approx \frac{0.56}{kl} = \frac{0.56\lambda}{2\pi l}. \]  

The proportionality of HWHM to the ratio λ/l is a direct consequence of the interference nature of coherent backscattering and has been verified in a lot of controlled laboratory experiments (e.g. Wolf et al., 1988). As follows from the theory of coherent backscattering (e.g. Ackermans et al., 1988; Ozrin, 1992a), in the case of finite-sized, anisotropically scattering grains, the scattering mean free path l must be replaced by the transport mean free path l0 given by l/(1 − g), where g is the asymmetry parameter of the phase function (for Rayleigh scatterers, g = 0 and l0 = l). Calculation of the transport mean free path and HWHM for sparsely packed media is rather straightforward. However, calculations for realistic, densely packed media require special attention since spatial correlation among scatterers can lead to a substantial increase of l0 as compared with sparsely distributed particles. Calculations of l0 and HWHM on the basis of a dense medium light-scattering theory, in which spatial correlation among scatterers is taken into account by intro-
grains are homogeneous spheres with radii governed by the standard gamma distribution (Hansen and Hovenier, 1974):
\[ n(r) \propto r^{(1 - 3b)/b} \exp\left[-r/(abh)\right], \]
(11)
where \( a \) is the effective radius and \( b \) is the effective variance. Also, we assume that the regolithic layer is optically thick (semi-infinite), the regolithic particles are nonabsorbing or weakly absorbing, and their index of refraction is in the interval [1.6, 1.7]. These assumptions are motivated by the following two reasons.

(1) Both 44 Nysa and 64 Angelina are high-albedo asteroids, and their surface is generally believed to be composed of a transparent dielectric material similar to the mineral enstatite with an index of refraction near 1.66 (e.g. Zellner, 1975; Zellner et al., 1977; Cloutis et al., 1990).

(2) Both absorption and the finite optical thickness of the scattering layer result in (strong) rounding off of the coherent backscattering peak (e.g. Etemad et al., 1987; Wolf et al., 1988), which otherwise has a distinct triangular shape near exactly the backscattering direction (Fig. 3). The measurements of Harris et al. (1989), which are characterized by a very small scatter of data points, do not show such a rounding off (Fig. 1). Therefore, it is reasonable to assume that at least those parts of the surface of the asteroids that are responsible for the observed opposition brightness are covered with an optically thick layer composed of nonabsorbing (or weakly absorbing) grains.

As is seen from Figs 1 and 3, the observed opposition peak has the same shape as that calculated from the theory of coherent backscattering. Therefore, to show that coherent backscattering of sunlight by the small regolithic grains can explain the unusually narrow opposition effect observed for the asteroids in the yellow, we must reproduce theoretically the observed amplitude of about 0.25 mag and angular semi-width of about 0.8° (see Fig. 1, lower panel).

The angular semi-width of the coherent opposition peak depends on four model parameters: the (real) refractive index \( N \) of the regolithic grains, a dimensionless size parameter \( y \) defined as the ratio of the effective grain radius to the wavelength of light, the effective variance \( b \), and filling factor \( f \) (i.e. the fraction of a volume occupied by the grains). In Figs 4–6, HWHM is plotted vs \( y \) for different values of \( f \), \( b \), and \( N \). In our calculations, we used a dense-medium light-scattering theory based on introducing the static structure factor (e.g. Wolf et al., 1988; Mishchenko, 1992b). It is seen from Figs 4–6, that whatever the grain refractive index is, HWHM has a peak near \( y = 0.5 \). The amplitude of the peak increases with increasing filling factor, decreasing width of the particle size distribution specified by the effective variance \( b \), and increasing refractive index. HWHM tends to zero with either \( y \to 0 \) or \( y \to \infty \). In practice this means that the coherent backscattering peak becomes unobservable for regolithic grains either much smaller or much larger than the wavelength. For \( y > 1 \), HWHM is almost independent of \( N \).

Unfortunately, Harris et al. (1989) report only yellow

3. Calculations

As was pointed out above, we assume that the surface of the asteroids 44 Nysa and 64 Angelina is (partly) covered with a layer of small regolithic grains producing the observed opposition effect via the coherent backscattering mechanism. For simplicity, we assume that the regolithic
calculated for the case of normal incidence of light on the surface. In the case of oblique incidence (e.g. near the limbs or due to macroscopic surface roughness), HWHM increases as $1/\cos \theta$ (Gorodnichenkov et al., 1990), where $\theta$ is the angle of incidence measured from the inward normal to the surface. Therefore, for a three-dimensional body with a macroscopically rough surface, the observed angular semi-width will be somewhat larger than that given by equation (10). Although it is practically impossible to calculate this enlargement accurately, a factor of about 1.5 seems to be a reasonable upper limit. Indeed, for a smooth, spherically symmetric body, the angle of incidence averaged over the illuminated surface at zero phase is equal to $45^\circ$, thus implying a factor of 1.4. The same factor follows from the assumption that rms surface roughness is close to $45^\circ$ (e.g. Lumme et al., 1985). Obviously, the combined effect of the global asteroid shape and surface roughness at zero phase will result in approximately the same or even weaker enlargement. As is seen from Figs 4–6, such an enlargement practically does not change the lower limit of possible grain radii, but slightly raises the upper limit.

The second quantity that specifies the opposition effect is the amplitude of the opposition spike $\zeta$, which is defined as the ratio of the total (i.e. diffuse + coherent) backscattered intensity at zero phase angle to the diffuse, background intensity:

$$\zeta = I_{\text{total}}/I_{\text{diffuse}} = [I_{\text{diffuse}} + I_{\text{coherent}}]/I_{\text{diffuse}}.$$ (12)

In the case of a macroscopically flat surface uniformly covered with the grains producing the coherent opposition effect, $\zeta = \zeta$, where $\zeta$ is given by equation (9). However, in the case of a (supposedly) nonuniform and macroscopically rough surface of the asteroids, $\zeta$ will be smaller than $\zeta$. Indeed, in this case the backscattered light can be divided into two parts of different origin. The first part comes from the light that is singly reflected in the opposite direction by unshadowed surface elements composed of the submicrometer-sized grains. This backscattered light results from the multiple-scattering processes that occur inside individual unshadowed surface elements with size of the order of the transport mean free path $l_{\text{t}}$. These multiple-scattering processes both contribute to the diffuse intensity and give rise to the observed coherent backscattering peak with HWHM $\approx 0.8^\circ$. The second part is the light that is (i) scattered by the surface elements composed of grains either much smaller or much larger than the wavelength and (ii) the light that is multiply reflected by different surface elements. These multiple reflections arise due to macroscopic surface roughness with scale much greater than $l_{\text{t}}$. The second part of the backscattered light contributes to the diffuse intensity but does not contribute to the observed opposition peak.

Precise calculations of the two components of the backscattered intensity are difficult because they require detailed information about the large-scale surface roughness, the fraction of the surface covered with the submicrometer-sized grains, and the size of the grains that cover the rest of the surface. Therefore, the only thing that we can do now is to verify that the observed amplitude of the opposition effect $\zeta$ is smaller than the amplitude $\zeta$ calculated theoretically for the light singly reflected by a

(V) magnitudes of the opposition effect for 44 Nysa and 64 Angelina. This makes the inversion problem ill posed and does not enable us to determine uniquely the size and refractive index of the grains producing the opposition effect. However, it is seen from Figs 4–6 that dielectric grains with index of refraction close to that of the mineral enstatite and effective radii from roughly 0.2 $\mu$m to roughly 0.7 $\mu$m can explain the observed angular semi-width of about $0.8^\circ$.

It should be noted here that the curves in Figs 4–6 are
The theoretically computed amplitude of the opposition effect $\zeta$ vs the angle of incidence. The optically thick (semi-infinite) medium with macroscopically flat surface is composed of polydisperse spherical particles with $a/\lambda = 1$, $N = 1.65$ and $b = 0.05$ (solid curve), 0.1 (dashed curve) and 0.2 (dot-dashed curve).

The enhancement factor for normal incidence $\zeta(0)$ is plotted vs the size parameter $y$ for $b = 0.1$ and $N = 1.6$, 1.65 and 1.7. Indeed we see that, in accordance with the conclusion of the preceding paragraph, the theoretically calculated amplitudes of about 1.4–1.6 are larger than the observed amplitude of about 0.25 mag in the yellow (Harris et al., 1989). This means that the fraction of the surface covered by the submicrometer-sized grains producing the opposition effect is less than unity and/or the multiple-reflection contribution due to macroscopic surface roughness is comparable with the single-reflection contribution.

4. Discussion and conclusions

Thus, we have shown in this paper that coherent backscattering of sunlight from an upper regolith layer which, apparently, partly covers the surfaces of the asteroids 44 Nysa and 64 Angelina and is composed of submicrometer-sized silicate grains, can produce the observed narrow and strong opposition spikes. We did not try here to find a unique solution for the parameters that specify the submicrometer-sized regolithic grains: $a$, $b$, $N$, $f$, and the fraction of the surface covered with these grains. Unfortunately, the observational data are not sufficient for this purpose. These parameters influence both the angular width and amplitude of the opposition spike, and the effect of one of these parameters can be compensated for by the effect of others. However, in our calculations we used a physical theory that has a rather strong physical background, involves direct physical parametrization in terms of the reproducible parameters $a$, $b$, $N$ and $f$, and has been verified in a lot of controlled laboratory experiments. Thus, although we were not able to prove that coherent backscattering is the explanation of the remarkable opposition brightening, we have demonstrated quantitatively that coherent backscattering can be a realistic explanation of this phenomenon.

As follows from our calculations, to produce the observed opposition peak via the coherent backscattering mechanism, the grains should have sizes of the order of the wavelength. Much larger or much smaller grains produce a coherent peak that is too narrow to be observed. It was shown in our recent paper (Mishchenko and Dlugach, 1992b) that the opposition effect observed for Saturn’s rings in the visible is, apparently, due to coherent backscattering of sunlight from a layer of submicrometer-sized ice grains which (partially) covers macroscopic ring particles. The same grains are known to produce the famous radial spokes in the outer B-ring of Saturn (Doyle and Grün, 1990) and may be responsible for the remarkable opposition effect observed for Europa and icy Uranian satellites (Mishchenko, 1992b). The possible origin of the submicrometer-sized regolithic grains at ice-covered atmosphereless surfaces at low temperatures is discussed by Smoluchowski (1983). It is still not clear if regolithic grains of the same size may be present at silicate airless surfaces. It is usually suggested that regolithic particles produced by meteoritic bombardment have radii of about 10 $\mu$m at the surface of the Moon and Mercury, and are much coarser at the surface of asteroids (e.g. Dollfus et al., 1989). However, as was shown by Zook and McCoy (1991), parts of the lunar surface may be covered by much finer, submicrometer-sized dust grains. If these grains are produced by a physical mechanism different from that discussed by Dollfus et al., it may well be that the same submicrometer-sized grains are also present on the surface of the asteroids 44 Nysa and 64 Angelina.

Finally we note that, as follows from Figs 4–6, the angular semi-width of the coherent backscatter opposition
effect is wavelength dependent. Therefore, spectral measurements of the opposition effect for the asteroids 44 Nysa and 64 Angelina would test if coherent backscattering is a likely explanation of the observed opposition spike and provide additional constraints on the size of the regolitic grains.

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