



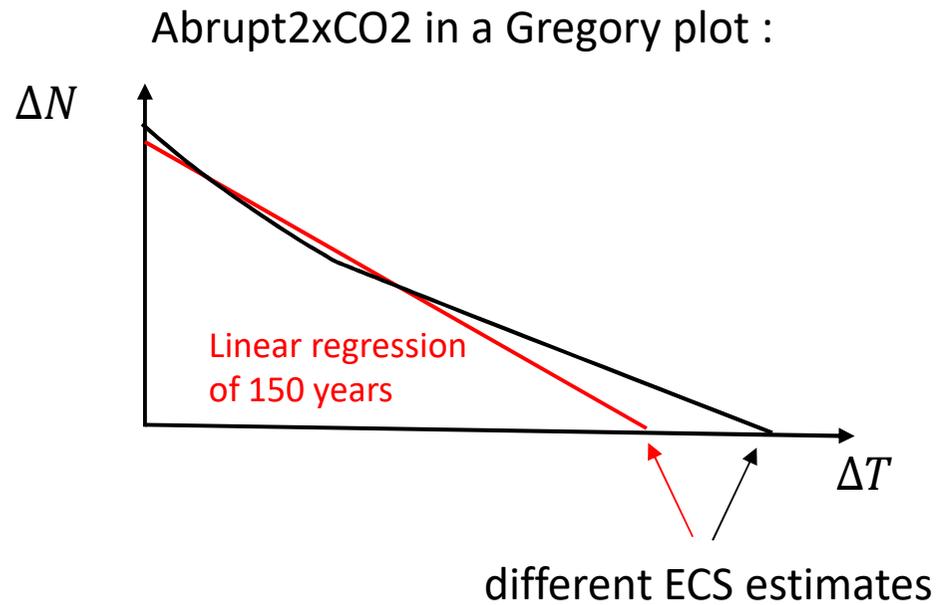
**Equilibrium- and transient- state dependencies of climate feedbacks:  
are they important for climate projections ?**

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CNRM, Météo-France / CNRS

CFMIP, 2019

## Some motivations



- Need to use same type of estimations when comparing models and obs
- (Any estimate of) ECS not necessary the best metric for warming in 2100
- They are other effects than the pattern effect : equilibrium-state dependencies

→ Are changing feedbacks important for constraining climate projections ?

## Outlines

- State dependencies of  $\lambda$  and CO<sub>2</sub>-forcing relationship in CMIP5 (+ CNRM-CM6.1)
- Importance for constraining climate projections ?

## Linear 2-layer energy balance model

**EBM** (*Gregory et al., 2000 ; Held et al., 2010*)

$$\begin{array}{l} \text{Upper ocean} \\ \text{+ atmo + land} \end{array} \quad C \frac{dT}{dt} = F - \lambda \Delta T - (\varepsilon - 1)H - H$$

$$\text{Deep ocean} \quad C_d \frac{dT_d}{dt} = H = \gamma (\Delta T - \Delta T_d)$$

**$\varepsilon \neq 1 \rightarrow$  pattern effect**

(*Winton et al., 2010; Held et al., 2010, Geoffroy et al., 2013b*)

# Linear 2-layer energy balance model

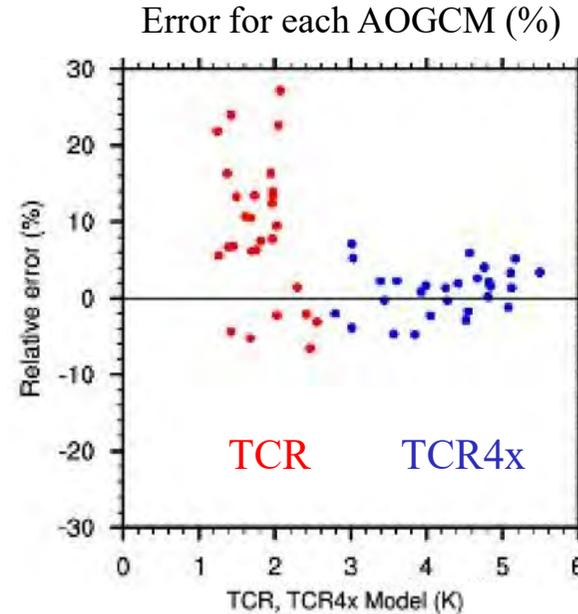
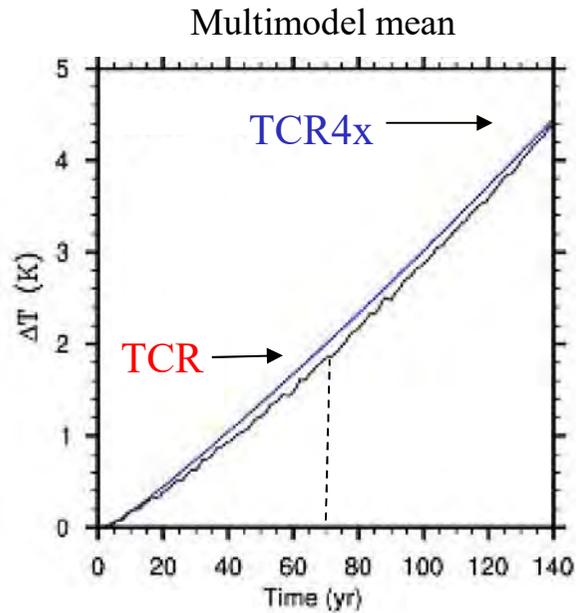
**EBM** (Gregory et al., 2000 ; Held et al., 2010)

Upper ocean + atmo + land  $C \frac{dT}{dt} = F - \lambda \Delta T - (\epsilon - 1)H - H$

Deep ocean  $C_d \frac{dT_d}{dt} = H = \gamma (\Delta T - \Delta T_d)$

**Log CO2-ERF relationship** (Myhre et al., 1998)

$$F(t) = F_4 \log_4 c(t) \quad \text{with } c = \frac{[CO_2]}{[CO_2]_0}$$

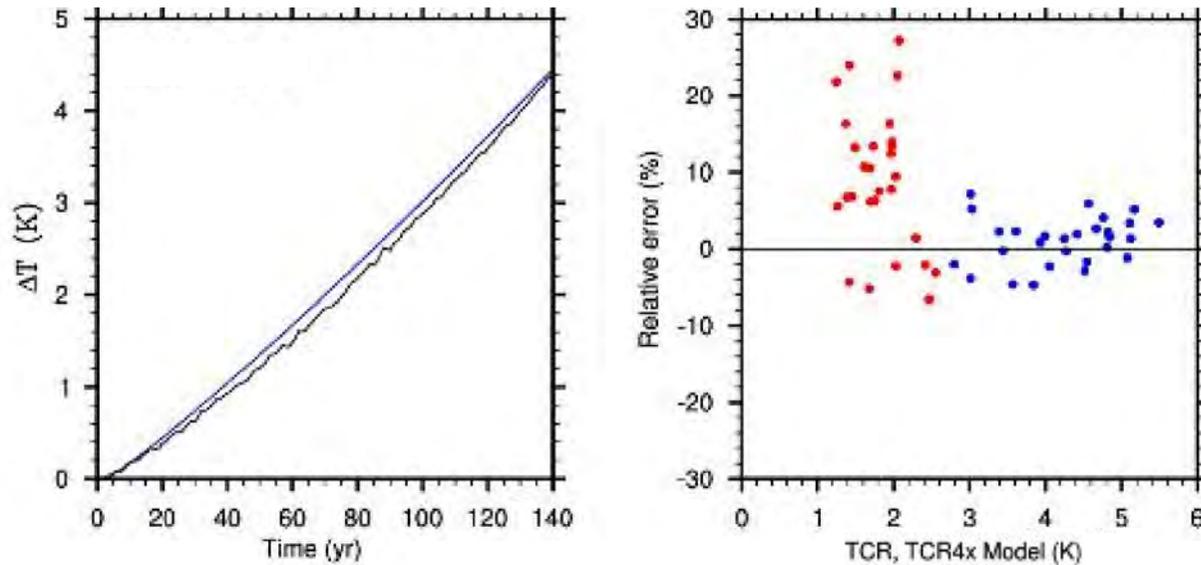


Calibration with abrupt4xCO2 →

**Overestimation of TCR**  
**Large spread**

## Linear 2-layer energy balance model

Log CO<sub>2</sub>-ERF relationship :



Quadratic CO<sub>2</sub>-ERF relationship from line-by-line RT model (BG14) :

$$F(t) = F_4 \left[ (1 - f) \log_4 c(t) + f (\log_4 c(t))^2 \right] \quad \text{with } c = \frac{[CO_2]}{[CO_2]_0}$$

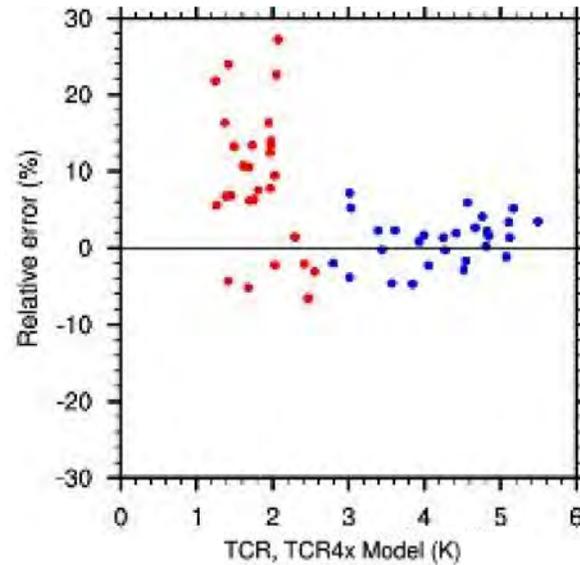
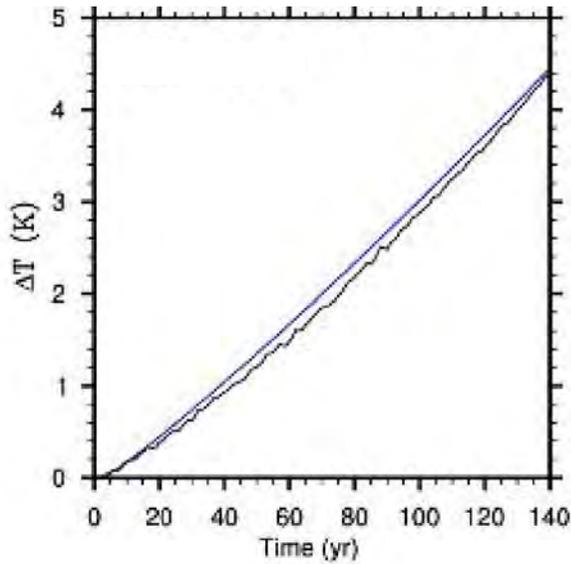
$f \approx 0.09$

(Byrne and Goldblatt, 2014, Etmann et al., 2016, Gregory et al., 2015)

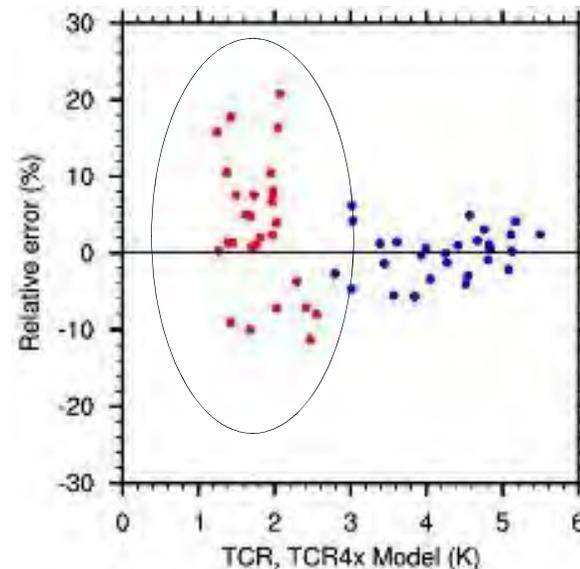
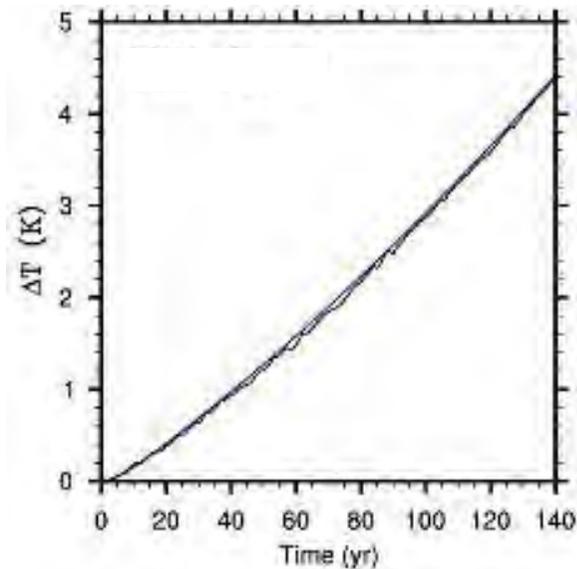
BG14

## Linear 2-layer energy balance model

Log CO<sub>2</sub>-ERF relationship :



Quadratic CO<sub>2</sub>-ERF relationship from line-by-line RT model (BG14) :



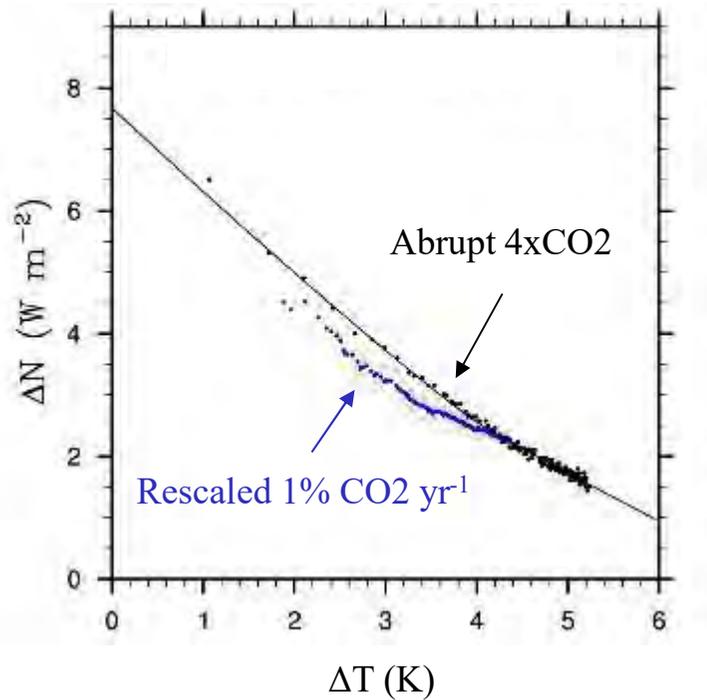
**Better agreement,  
large spread**

*In agreement with  
Gregory et al. (2015)*

# Rescaled 1% CO<sub>2</sub> yr<sup>-1</sup> in order to match the abrupt4xCO<sub>2</sub>

$$\Delta N = F(t) - \lambda \Delta T \quad \xrightarrow{\quad \times \frac{F_{4\times}}{F(t)} \quad} \quad \frac{F_{4\times}}{F(t)} \Delta N = F_{4\times} - \lambda \frac{F_{4\times}}{F(t)} \Delta T$$

Log forcing



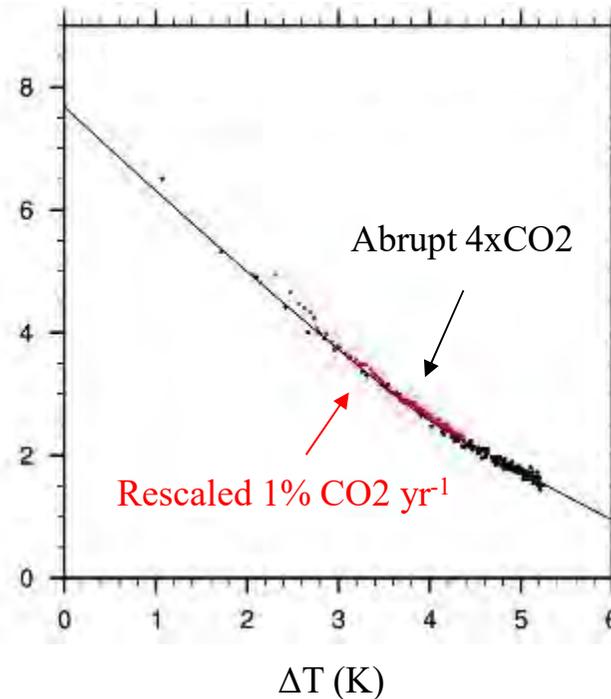
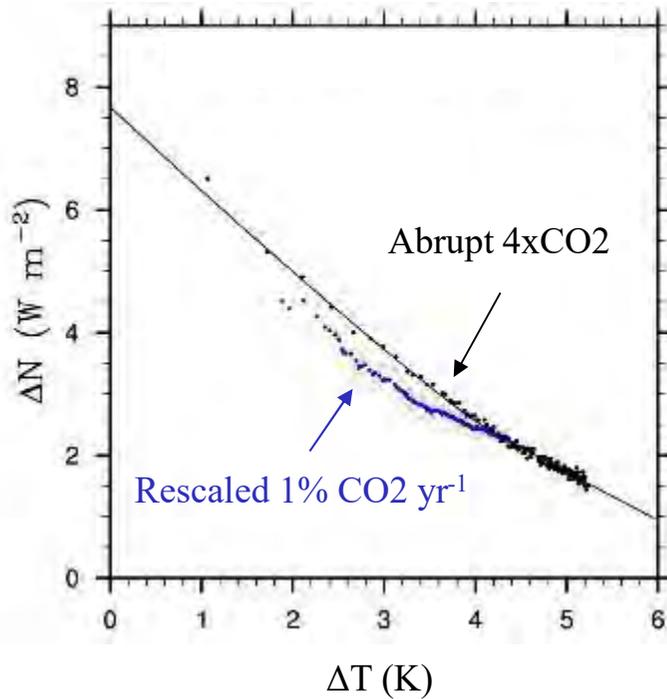
# Rescaled 1% CO2 yr<sup>-1</sup> in order to match the abrupt4xCO2

$$\Delta N = F(t) - \lambda \Delta T \quad \xrightarrow{\quad} \quad \frac{F_{4\times}}{F(t)} \Delta N = F_{4\times} - \lambda \frac{F_{4\times}}{F(t)} \Delta T$$

$$\times \frac{F_{4\times}}{F(t)}$$

Log forcing

Quadratic forcing from BG14

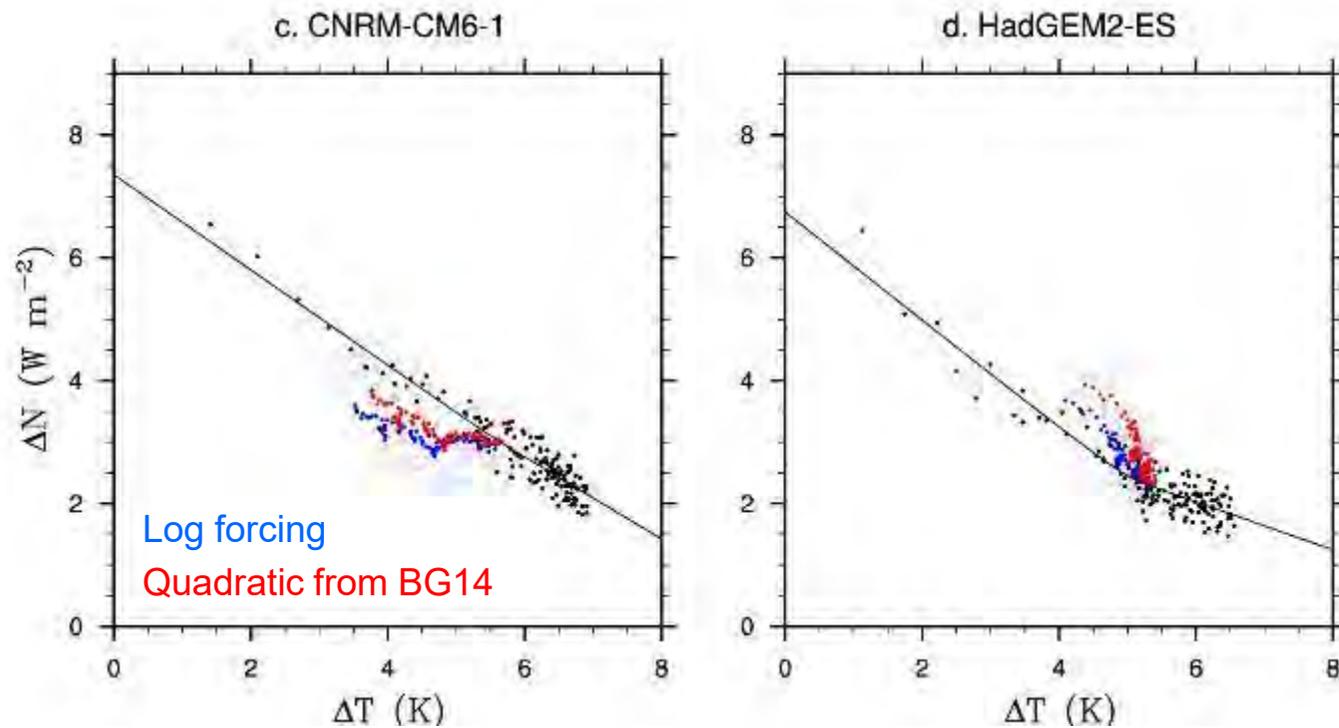


Good representation

*In agreement with Gregory et al. (2015)*

## Rescaled 1% CO<sub>2</sub> yr<sup>-1</sup> in order to match the abrupt4xCO<sub>2</sub>

Large spread :



Difference due to CO<sub>2</sub>-ERF relationship and/or equilibrium state dependency of  $\lambda$

# CO<sub>2</sub>-ERF relationship and equilibrium state dependency of $\lambda$ in an EBM

	EBM 1	EBM 2	EBM 3
Quadratic ERF $F_4 [ (1 - f) \log_4 c + f (\log_4 c)^2 ]$	f model dependent	f from BG14 (f ≈ 0.09)	f from BG14 (f ≈ 0.09)
$\lambda$	Constant	f([CO <sub>2</sub> ])	f( $\Delta T$ )

$$\lambda = \lambda_4 [ (1 - g_c) + g_c \log_4 c ]$$

$$\lambda = \lambda_0^T [ (1 - g_T) + g_T \frac{\Delta T}{ECS_0} ]$$

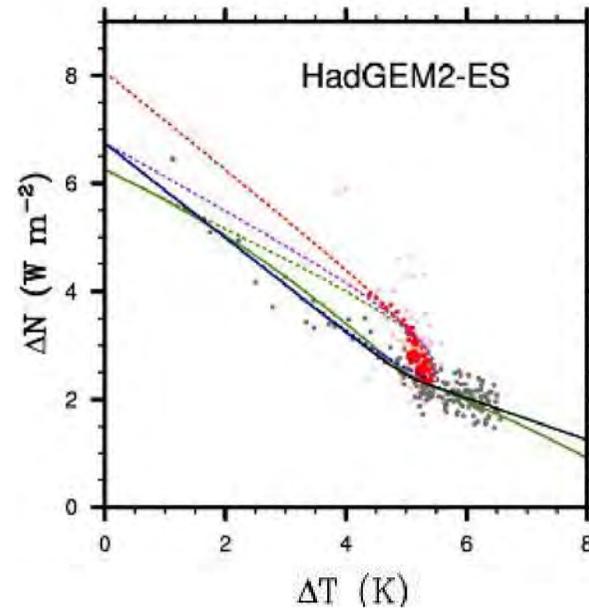
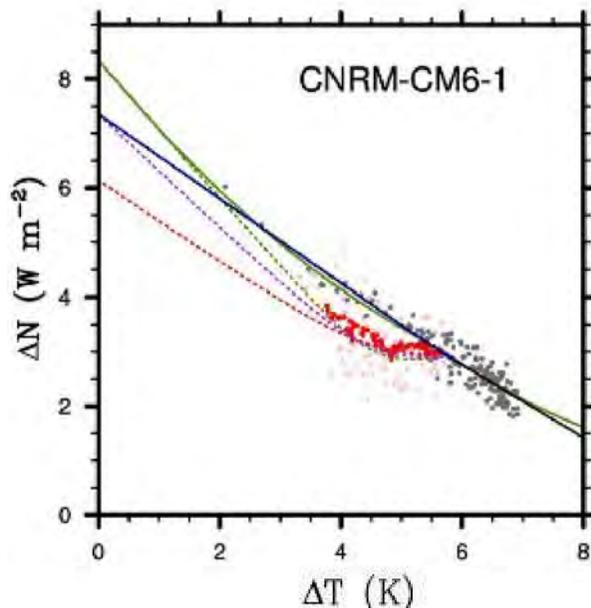
Equilibrium state dependencies of  $\lambda$

(Colman et al., 1997; Jonko et al. 2012, Block and Mauritsen, 2013; Bloch-Johnson et al., 2015)

# CO<sub>2</sub>-ERF relationship and equilibrium state dependency of $\lambda$ in an EBM

	EBM 1	EBM 2	EBM 3
Quadratic ERF $F_4 [ (1 - f) \log_4 c + f (\log_4 c)^2 ]$	f model dependent	f from BG14 (f $\approx$ 0.09)	f from BG14 (f $\approx$ 0.09)
$\lambda$	Constant	f([CO <sub>2</sub> ])	f( $\Delta T$ )

Effects can not be dissociated  $\rightarrow$  Assume one single effect fully explain the nonlinear behaviour

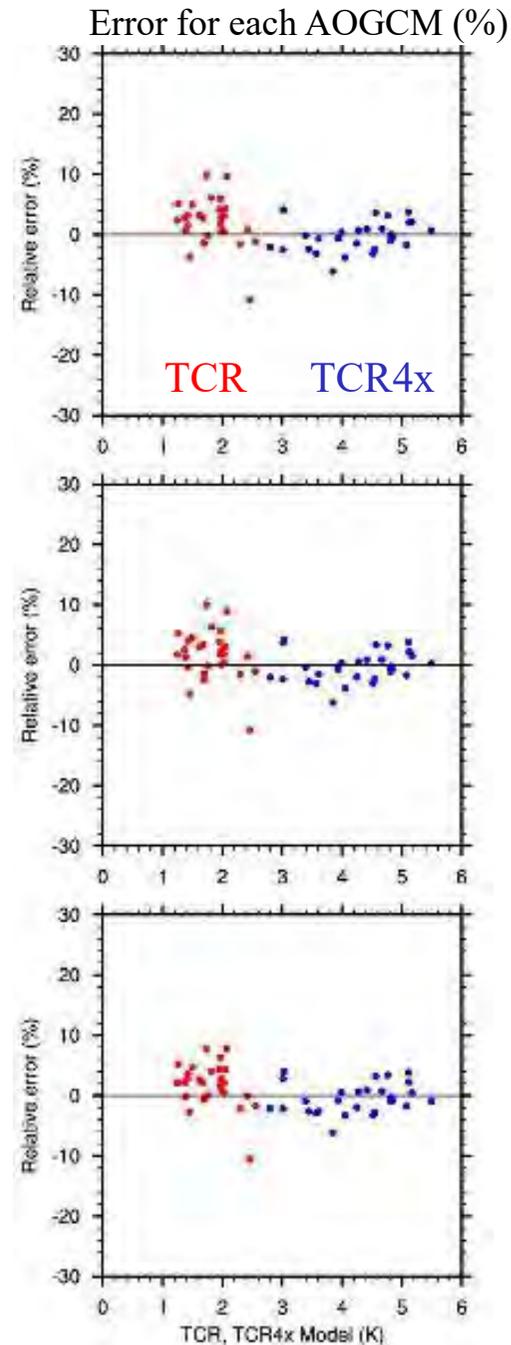
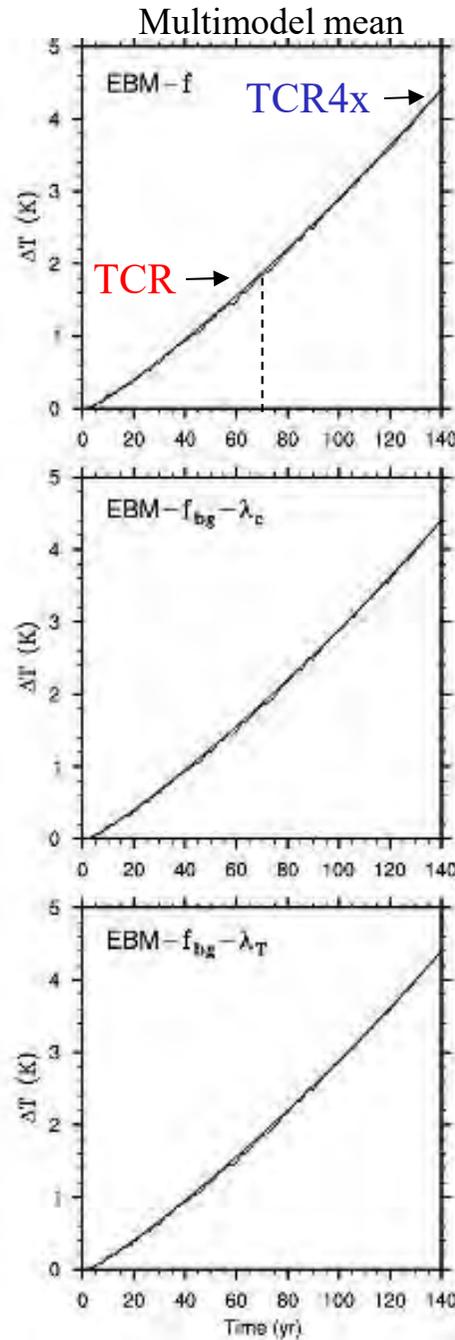


# Representation of the 1% CO<sub>2</sub> yr<sup>-1</sup> by each EBM

- Quadratic ERF
- $\lambda = \text{constant}$

- Quadratic ERF from BG14
- $\lambda = f([\text{CO}_2])$

- Quadratic ERF from BG14
- $\lambda = f(\Delta T)$



Similar reduction of the spread

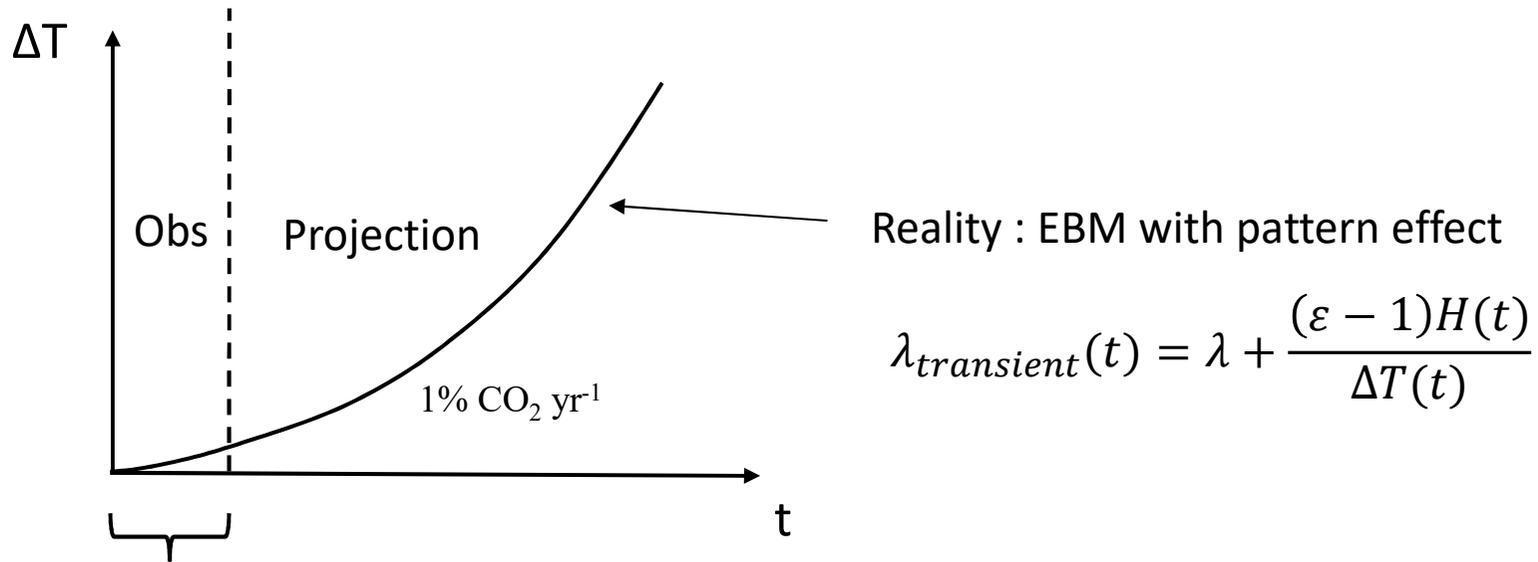
## Outlines

- State dependencies of  $\lambda$  and CO<sub>2</sub>-forcing relationship in CMIP5

### **- Importance of CO<sub>2</sub>-ERF relationship and state dependencies of $\lambda$ for constraining climate projections ?**

- Use idealized scenarios
- Use the 2-layer EBM calibrated with CMIP5 models as a perfect model

## Importance of pattern effect for constraining climate projections : method



Assume we can measure  $\lambda_{transient}$  but not  $\lambda$  and  $\varepsilon$

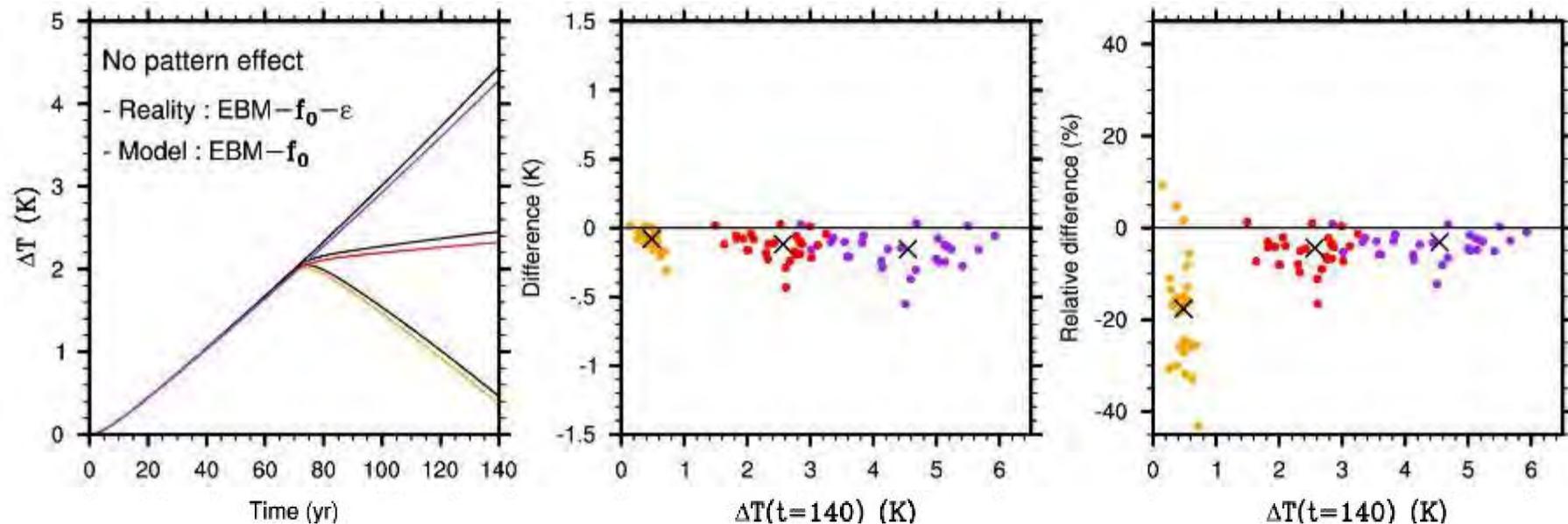
Projection with  $\lambda_{transient} = cste = \text{observed value}$  → Error in projected warming ?

Use the value at  $t \rightarrow 0$

## Importance of pattern effect for constraining climate projections

Reality : EBM with **pattern effect**  $\lambda_{transient}(t) = \lambda + \frac{(\varepsilon - 1)H(t)}{\Delta T(t)}$

Estimation : EBM with **constant**  $\lambda_{transient}$  estimated at  $t \rightarrow 0$  yr



Neglecting the pattern effect to constrain TCR4x  $\rightarrow$  **median relative error of only 3 %**

## Importance of CO<sub>2</sub>-ERF relationship and/or equilibrium state dependent $\lambda$

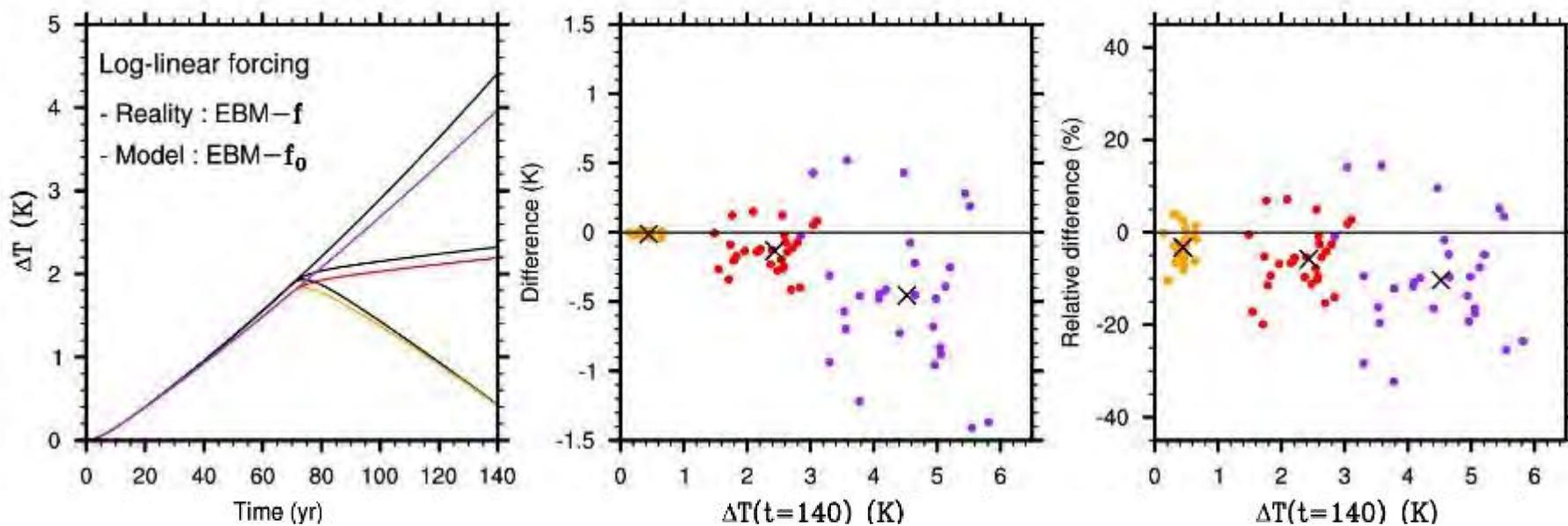
Effects can not be dissociated

→ Use one EBM with one single effect  
and assume it well represents all the 3 effects

## Importance of CO<sub>2</sub>-ERF relationship and/or equilibrium state dependent $\lambda$

Reality : EBM with **quadratic forcing with f model dependent**  $F_4 [(1 - f)\log_4 c + f (\log_4 c)^2]$

Estimation : EBM with **Log forcing** with  $F_4$  estimated at  $t \rightarrow 0$

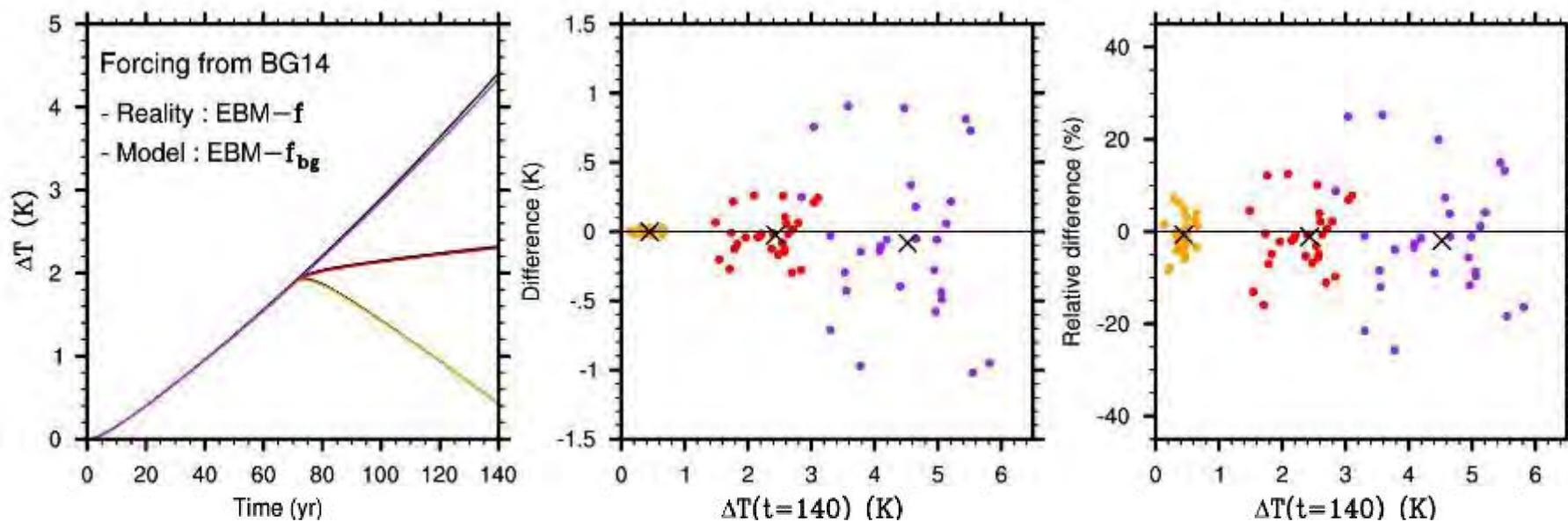


**→ Median error = -10 % , large spread**

## Importance of CO2-ERF relationship and/or equilibrium state dependent $\lambda$

Reality : EBM with **quadratic forcing with f model dependent**  $F_4 [(1 - f)\log_4 c + f (\log_4 c)^2]$

Estimation : EBM with **BG14 quadratic forcing** with  $F_4$  estimated at  $t \rightarrow 0$

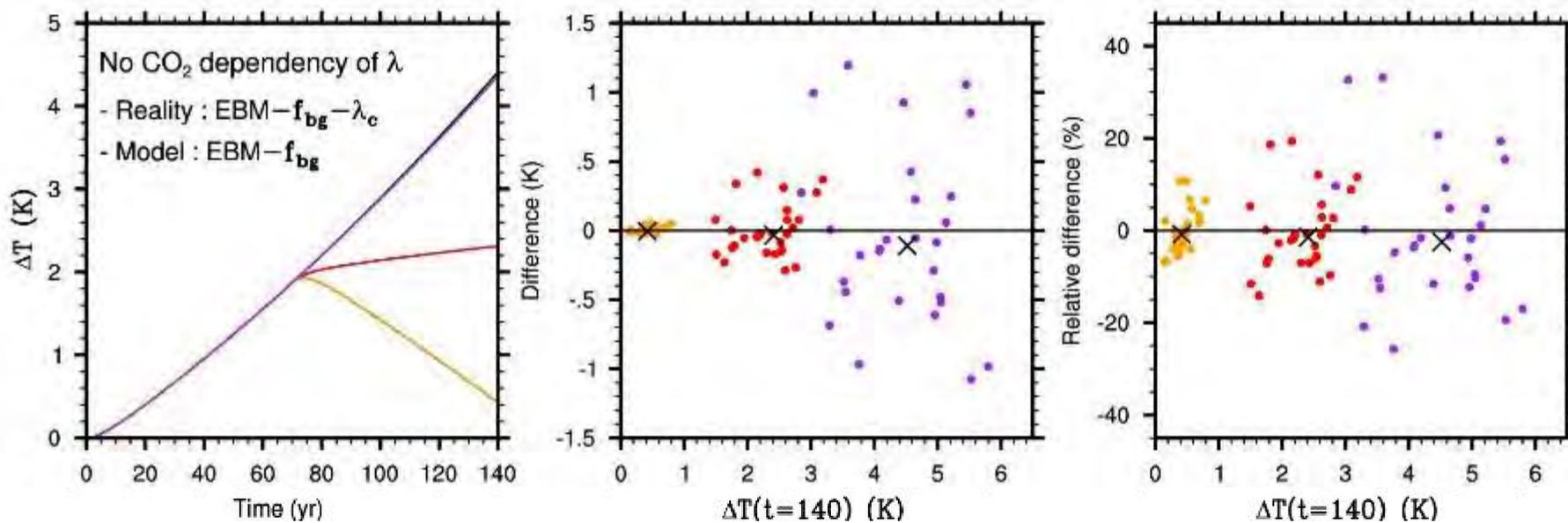


→ Median error = 0 % , large spread

## Importance of CO<sub>2</sub>-ERF relationship and/or equilibrium state dependent $\lambda$

Reality : EBM with BG14 quadratic forcing and **CO<sub>2</sub>-dependent  $\lambda$**

Estimation : EBM with BG14 quadratic forcing and **constant  $\lambda$**  estimated at  $t \rightarrow 0$

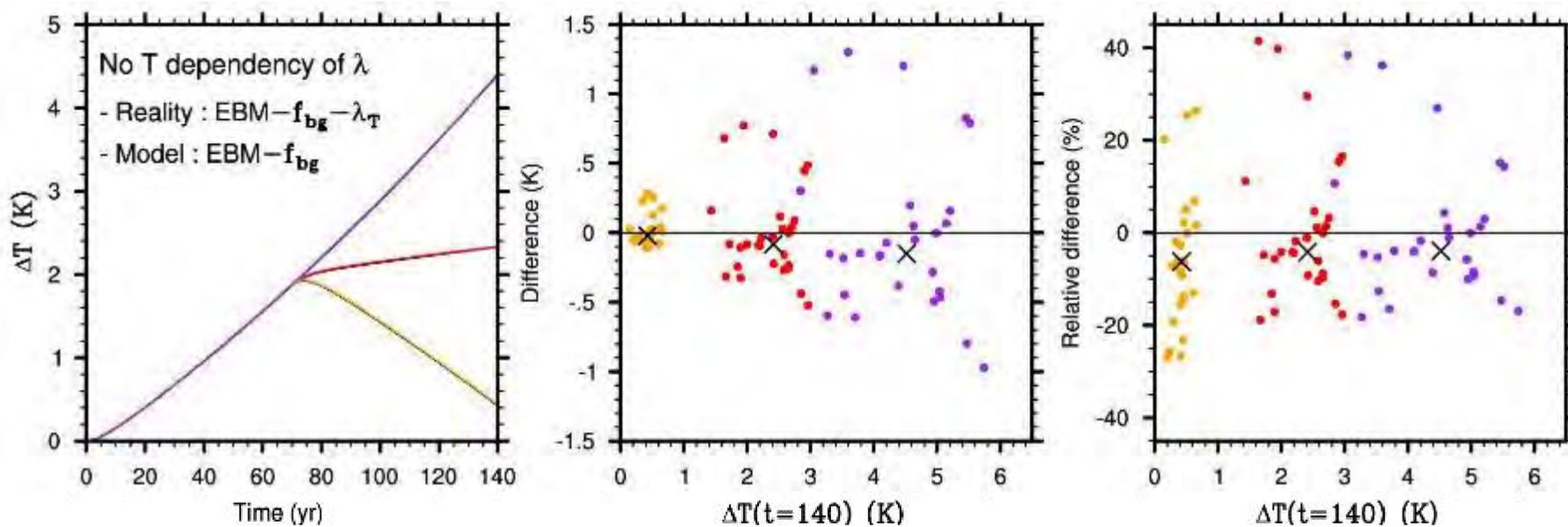


**→ Same results : median error = 0 % , large spread**

## Importance of CO<sub>2</sub>-ERF relationship and/or equilibrium state dependent $\lambda$

Reality : EBM with BG14 quadratic forcing and **T-dependent  $\lambda$**

Estimation : EBM with BG14 quadratic forcing and **constant  $\lambda$**  estimated at  $t \rightarrow 0$



**→ Similar results : median error = 0 % , large spread**

## Conclusion

- 2-layer EBM with pattern effect calibrated from abrupt4xCO<sub>2</sub>,  
+ **quadratic forcing from line-by-line RT models** → median TCR well represented

Large spread due to i) deviation from BG14 forcing

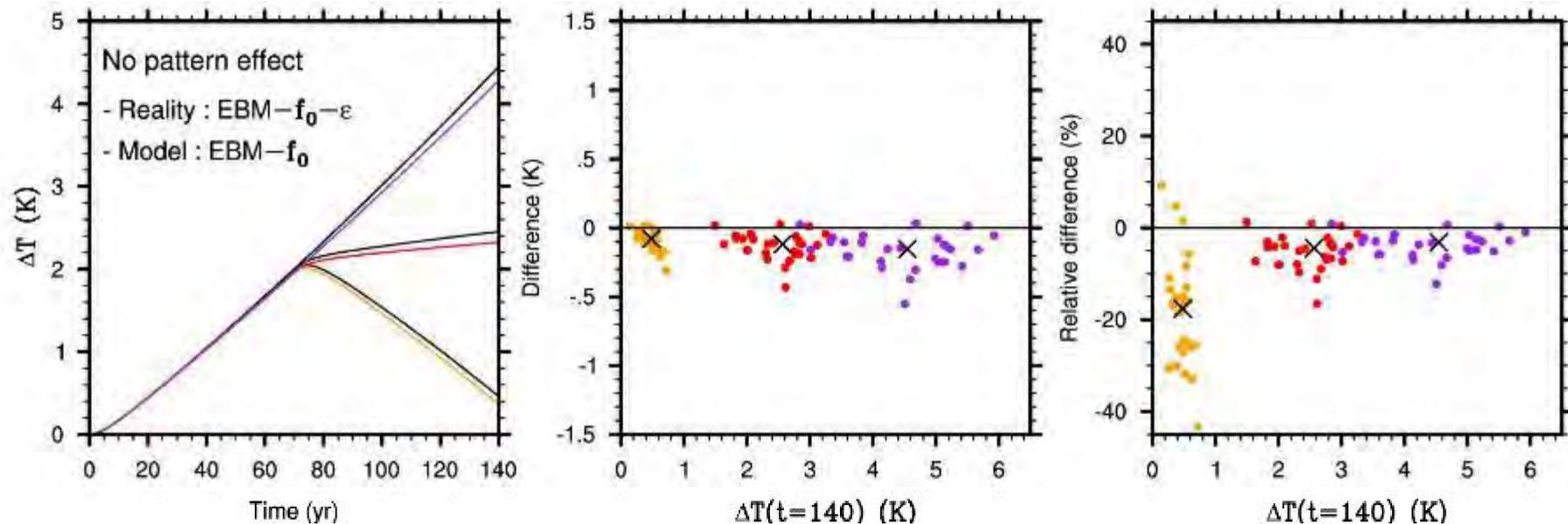
ii) equilibrium-state dependencies of  $\lambda$  (on CO<sub>2</sub>, T)

- Importance for constraining climate projections (use TCR<sub>4x</sub>,  $\Delta T_{\text{stabilization}}$ ,  $\Delta T_{\text{ramp-down}}$ )  
→ **The (forced) pattern effect** is not important (3 % of error for TCR<sub>4x</sub>)  
→ If AOGCMs correctly represent BG14 forcing, a **log forcing** lead to a error of -10 %  
→ **Equilibrium state dependencies and/or deviation from BG14 forcing**  
do not induce any systematic error when a BG14 forcing is used,  
but contribute to increase uncertainties

## Importance of pattern effect for constraining climate projections

Reality : EBM with pattern effect  $\lambda_{transient}(t) = \lambda + \frac{(\varepsilon - 1)H(t)}{\Delta T(t)}$

Estimation : EBM with constant  $\lambda_{transient}$  with value « measured » at  $t \rightarrow 0$  yr

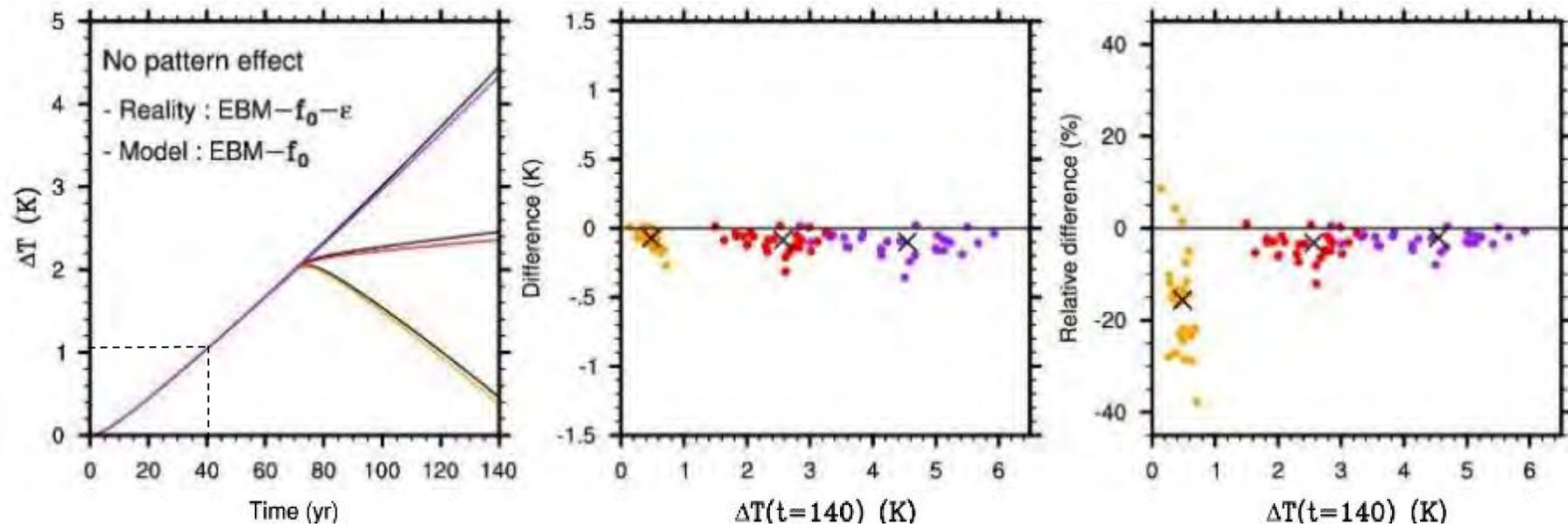


Neglecting the pattern effect to constrain TCR4x  $\rightarrow$  **median relative error of only 3 %**

## Importance of pattern effect for constraining climate projections

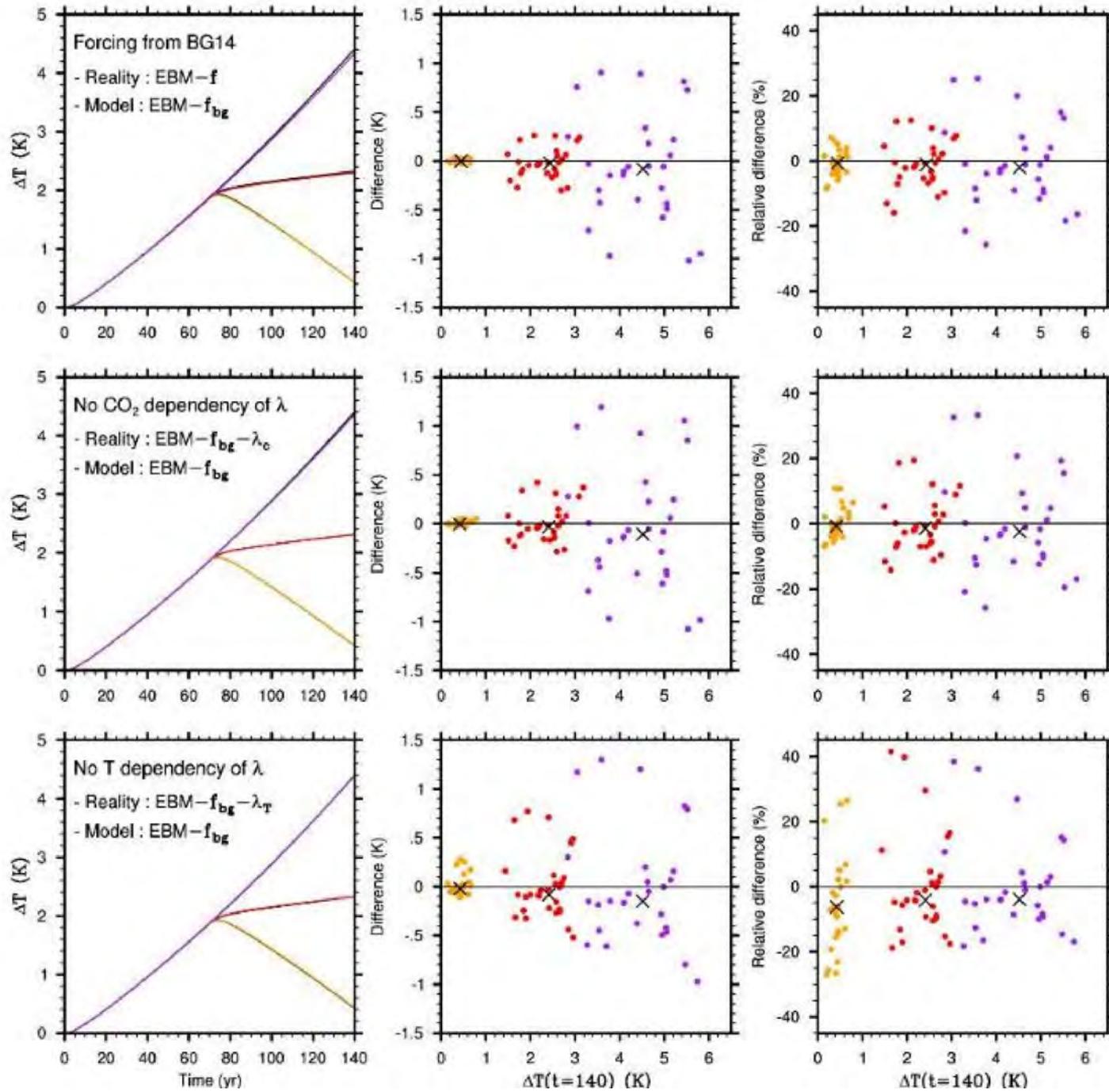
Reality : EBM with pattern effect  $\lambda_{transient}(t) = \lambda + \frac{(\varepsilon - 1)H(t)}{\Delta T(t)}$

Estimation : EBM with constant  $\lambda_{transient}$  with value « measured » at **t = 40 yr**

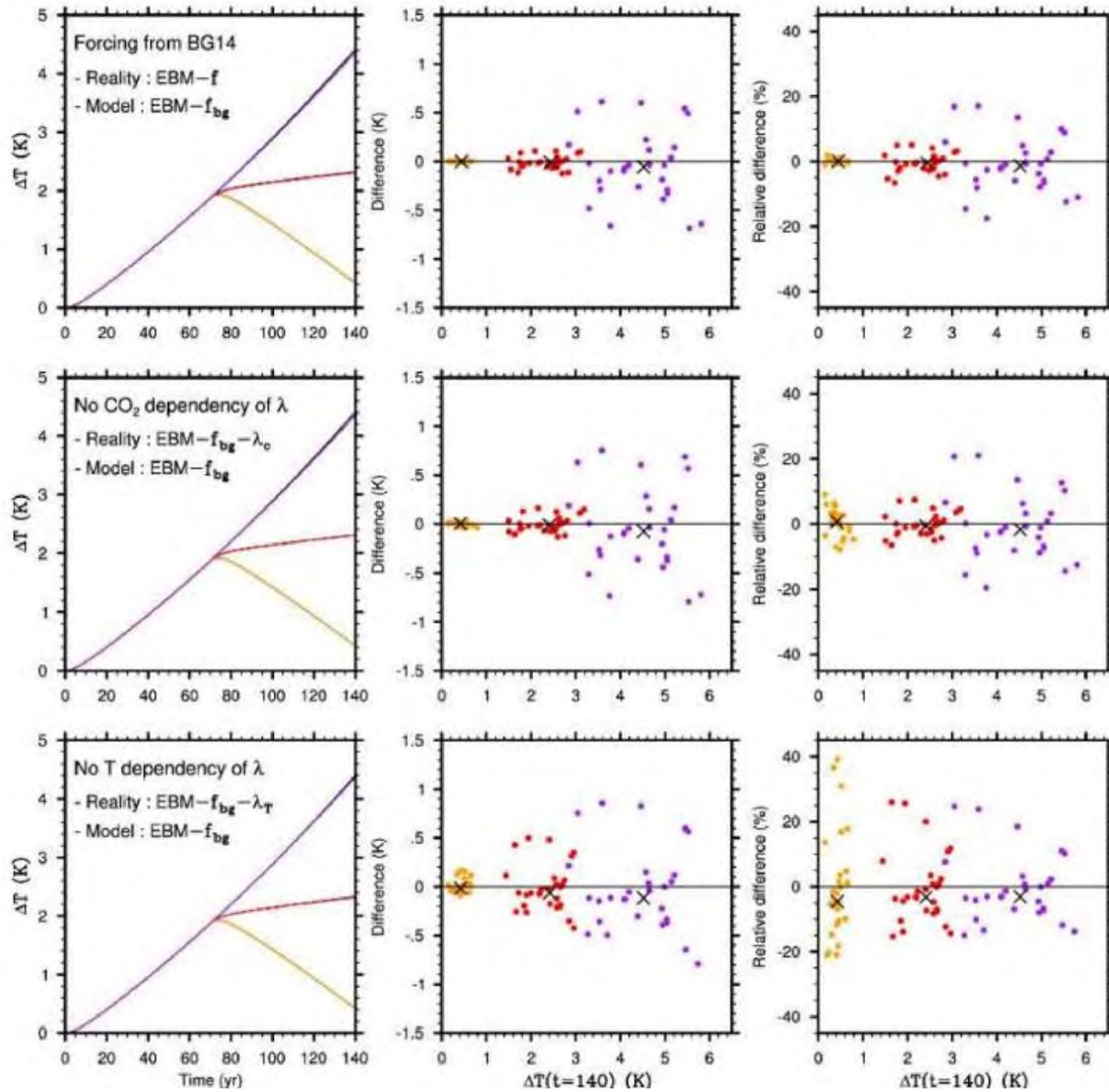


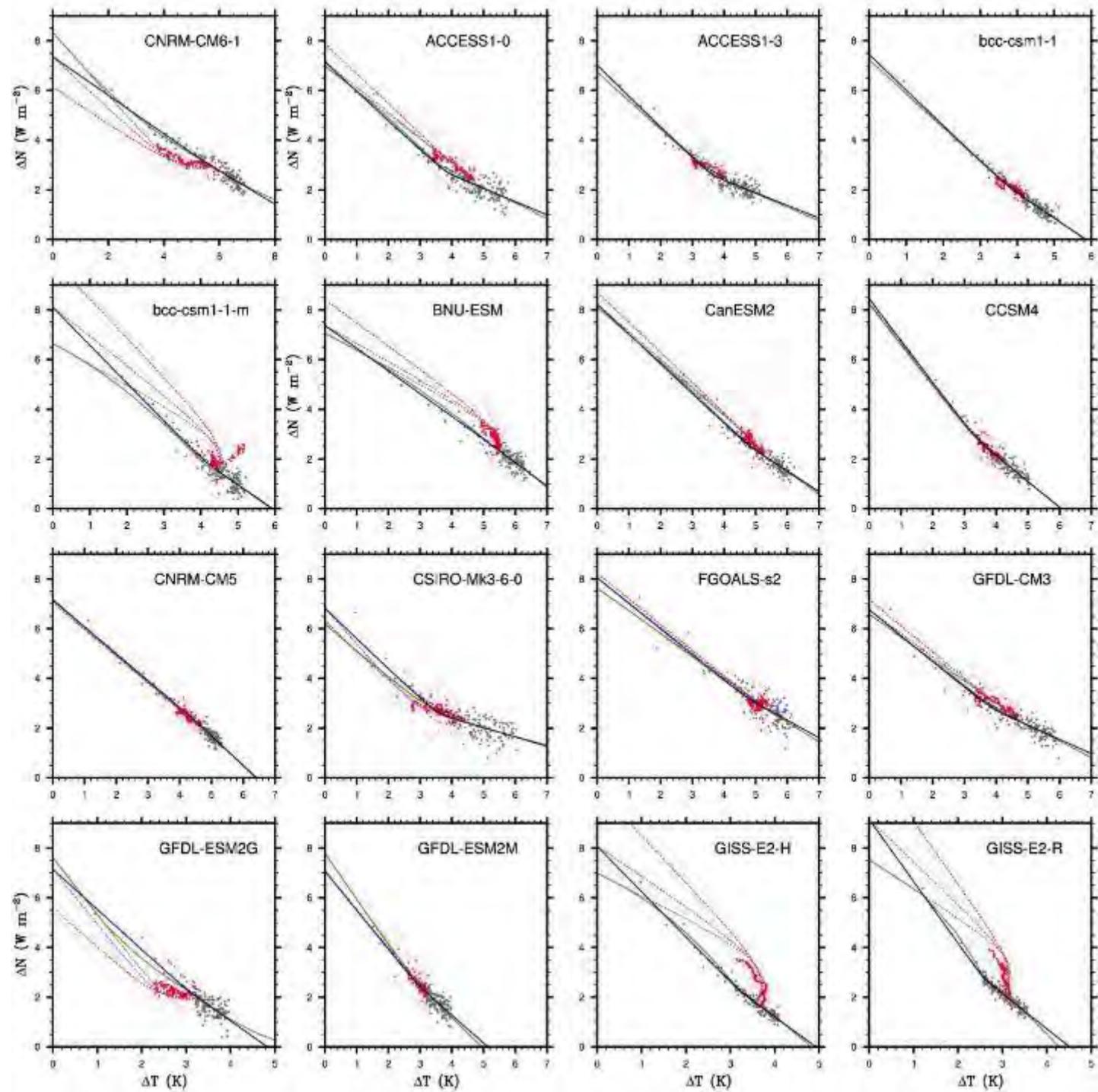
Neglecting the pattern effect to constrain TCR4x  $\rightarrow$  **median relative error of only 3 %**

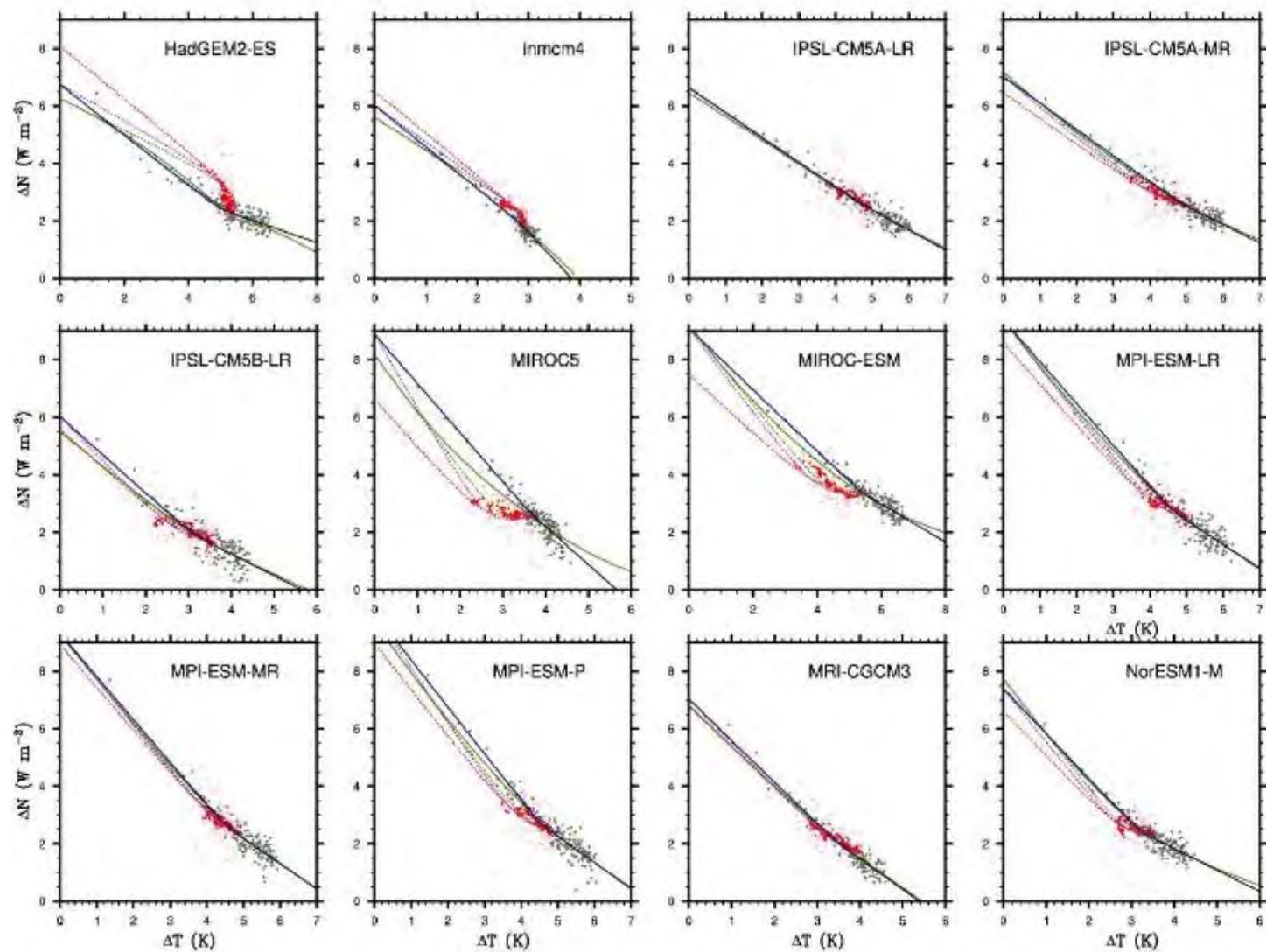
$t \rightarrow 0$  yr



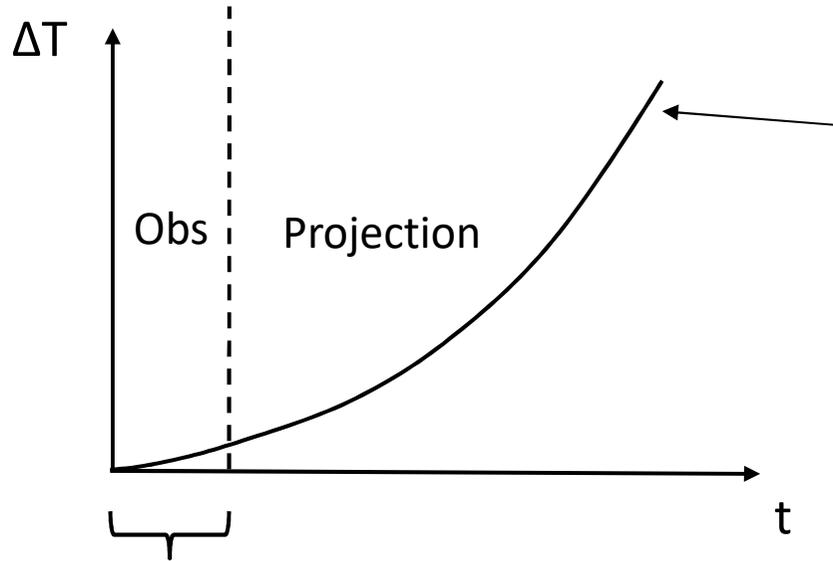
$t = 40 \text{ yr}$







## Importance of pattern effect for constraining climate projections



Reality : EBM with pattern effect

$$\lambda_{transient} = \lambda + \frac{(\varepsilon - 1)H}{\Delta T}$$

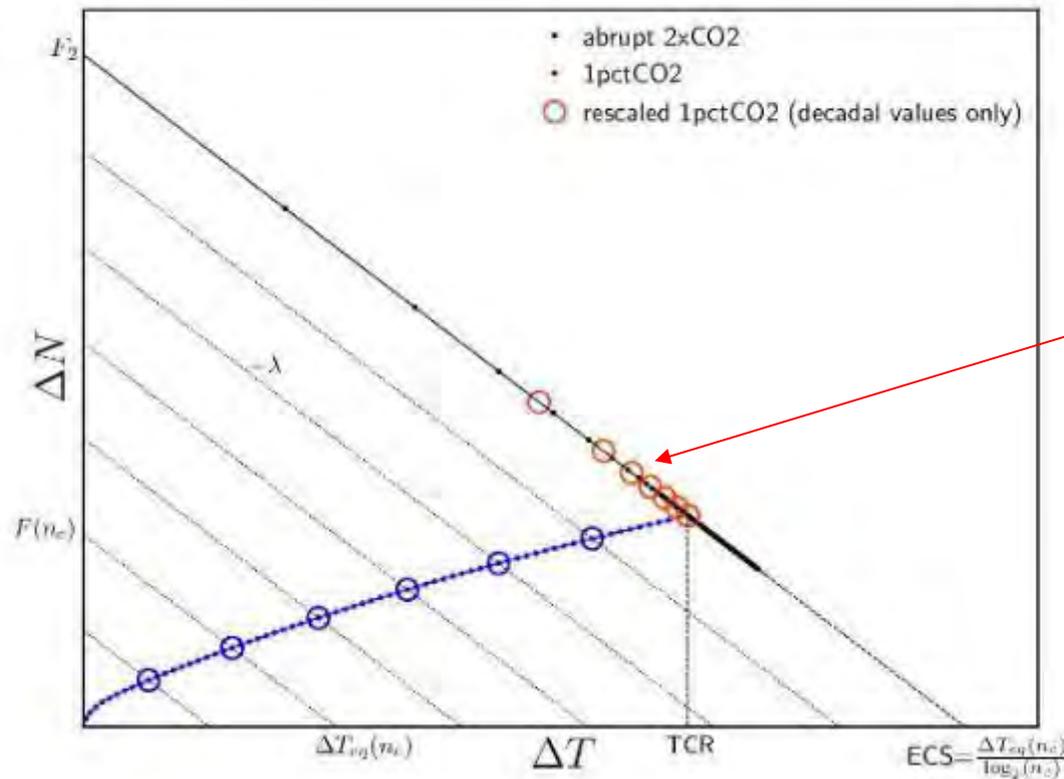
Assume we can measure  $\lambda_{transient}$  but not  $\varepsilon$

Projection with  $\lambda_{transient} = cste = \text{observed value}$  → Error in projected warming ?

Use the limit of  $t=0$  :  
 $= \lambda + (1 - \varepsilon)\gamma$

# Linear forcing feedback framework

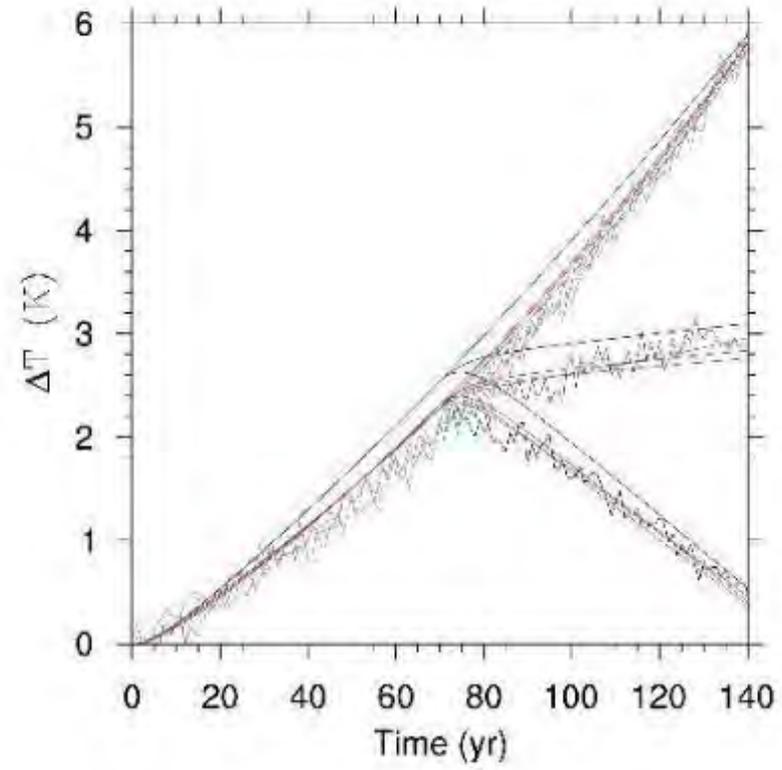
$$\Delta N = F(t) - \lambda \Delta T \quad \xrightarrow{\text{rescaling}} \quad \frac{F_{2\times}}{F(t)} \Delta N = F_{2\times} - \lambda \frac{F_{2\times}}{F(t)} \Delta T$$



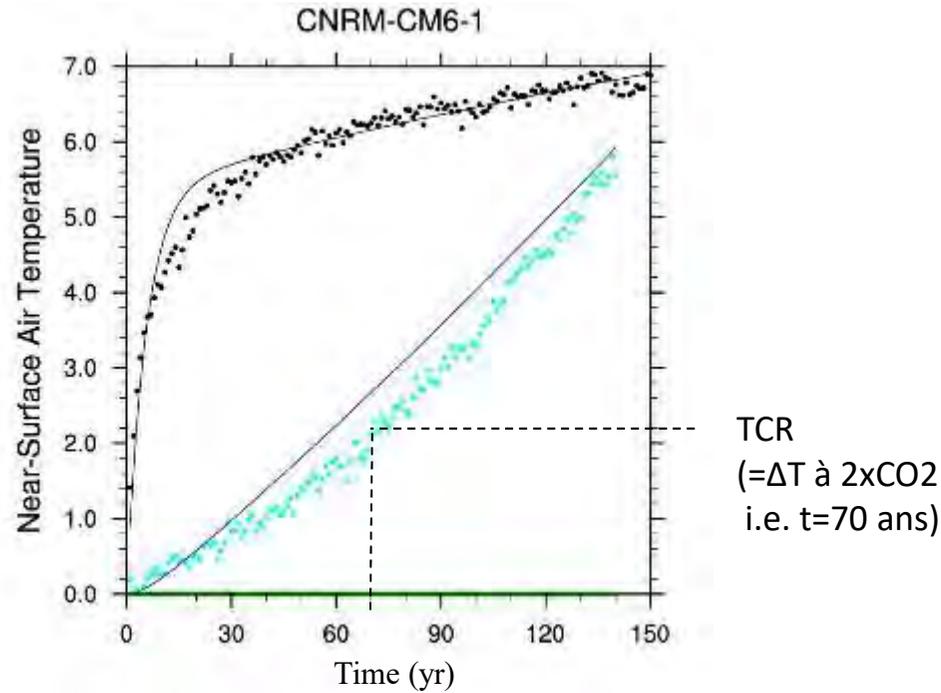
$$(\Delta T, \Delta N) \times \frac{F_{2\times}}{F(t)}$$

Any deviation from the abrupt2xCO2 line shows a limitation of the linear F- $\lambda$  framework

CNRM-CM6-1



## Limitation de l'EBM (avec ou sans $\epsilon$ ) : biais TCR



Probablement en lien :  
 $\Delta T(t=2100)$  dans un RCP8.5  
mieux corrélé à « ECS » qu'à TCR  
(*Große et al. 2018*)

Explications possibles :

- forçage pas en  $\log(\text{CO}_2)$ ,
- $\lambda$  non constant (autre que pattern effect)
- Param de H

} radiatif  
} OHU